

## Parts 3-6 are EXAMPLES for cse634

### FINAL TEST CSE 352 ARTIFICIAL INTELLIGENCE Fall 2008

- There are 6 pages in this exam. Please make sure you have all of them
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#### INTRODUCTION – Philosophical AI Questions

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- Q1.** Write some pro and contra arguments about TURING TEST as the test of artificial intelligence.
- Q2.** Describe some technological “science fiction” inventions in your favorite Science Fiction movie that are realistic as of today’s state of technology, and some others that are not realistic.

#### PART ONE –Expert Systems

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- Q1.** Write a simple (5-6 rules long) Expert System (in English) for a task (or tasks) chosen by you.
- Q2.** Conceptualize your system in PROPOSITIONAL LOGIC.
- Q3.** Pose some questions to your system in order to build a database of FACTS related to your task and use backward chaining to show if your task succeeds, or fails depending on the answers to the questions.

HINT: Look at Hmk1part1 solutions and our book.

#### PART TWO – Resolution and Predicate Logic

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- Q1.** Write all resolvents of  $\Delta = \{ \{a, \neg a, \neg b, c\}, \{a, b\}, \{ \neg b, \neg c\}, \{b\} \}$
- Q2.** Apply all possible Resolution Strategies (state which are complete) to verify whether the set  $\Delta$  below is satisfiable, or not.

$$\Delta = \{ \{a, \neg b\}, \{ \neg a, \neg b \}, \{b, c\}, \{a, \neg c\}, \{ \neg a \}, \{a, b, \neg a \}, \{ \neg b, a, c, b \}, \{b\}, \{c\} \}$$

- Q3.** Use resolution deduction (and completeness of your resolution strategy) to decide the validity of the following argument.

From

$$A1: ((a \rightarrow (\neg b \wedge c)) \rightarrow (b \rightarrow \neg a)) \vee ((a \rightarrow \neg c) \vee b) \text{ and}$$

$$A2: (a \rightarrow b) \rightarrow a,$$

we deduce that

$$B: ( \neg(a \rightarrow (\neg b \wedge c)) \rightarrow (a \wedge (b \wedge \neg c)) )$$

**Q4.** Prove the following Law of Quantifiers

$$(\forall x A(x) \cup \forall x B(x)) \Rightarrow \forall x (A(x) \cup B(x))$$

Give an example of a non empty domain X and formulas A(x), B(x),  
For which the  $\Leftarrow$  direction does not hold.

**Q5. (a)** Translate the following sentences into Predicate Logic and AI Logic under intended interpretation. Write down your choice of predicates.

A1: All flowers are blue and pretty.

A2: All blue flowers are pretty.

A3: All flowers are pretty.

(b) Decide whether the ARGUMENT:  $A1 \wedge A2 \Rightarrow A3$  is VALID, or NOT VALID.  
Show work.

**Q6. (a)** Translate the following sentences into Predicate Logic and AI Logic under intended interpretation. Write down your choice of predicates.

A1: All students are clever.

A2: Some clever students have blue eyes.

A3: There is a student with blue eyes.

(b) Decide whether the ARGUMENT:  $A1 \wedge A2 \Rightarrow A3$  is VALID, or NOT VALID.  
Show work.

## **PART THREE – Classification Rules**

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### **Definition 1**

Given a classification dataset DB with a set  $A = \{a_1, a_2, \dots, a_n\}$  of attributes and a class attribute C with values  $\{c_1, c_2, \dots, c_k\}$  (k classes), any expression;

$a_1 = v_1 A \dots \wedge a_k = v_k$ , where  $a_i \in A$  and  $v_i$  are corresponding values of attributes,

is called attributes DESCRIPTION, for short a DESCRIPTION.

The expression  $C = c_k$  is called a class DESCRIPTION, for short a CLASS.

### **Definition 2**

A CHARACTERISTIC FORMULA is any expression

$C = c_k \Rightarrow a_1 = v_1 \wedge \dots \wedge a_k = v_k$ , or shortly we write it as CLASS  $\Rightarrow$  DESCRIPTION.

**Definition 3**

A DETERMINANT formula is any expression

$a_1 = v_1 \wedge \dots \wedge a_k = v_k \Rightarrow C = c_k$ , or shortly a formula  
DESCRIPTION  $\Rightarrow$  CLASS.

**Definition 4**

A characteristic formula CLASS  $\Rightarrow$  DESCRIPTION is called a CHARACTERISITIC RULE of a given dataset DB iff it is **TRUE** in DB, i.e. when the following condition holds

$$\{o: \text{DESCRIPTION}\} \cap \{o: \text{CLASS}\} \neq \emptyset,$$

Where  $\{o: \text{DESCRIPTION}\}$  is the set of all records of DB corresponding to the Attributes DESCRIPTION,  $\{o: \text{CLASS}\}$  is the set of all records of DB corresponding to the CLASS description.

**Definition 5**

A discriminant formula DESCRIPTION  $\Rightarrow$  CLASS is called a DISCRIMINANT RULE for a given **DB** iff it is **TRUE in the DB**, i.e. the following holds

1.  $\{o: \text{DESCRIPTION}\} \neq \emptyset$
2.  $\{o: \text{DESCRIPTION}\} \subseteq \{o: \text{CLASS}\}$

**Q1.** Prove that for any data base DB, for any of its DISCRIMINANT rules

DESCRIPTION  $\Rightarrow$  CLASS, the formula

CLASS  $\Rightarrow$  DESCRIPTION is a characteristic RULE for the DB, but not vice-versa.

See lecture notes for an example of a characteristic rule CLASS  $\Rightarrow$  DESCRIPTION such that the corresponding formula DESCRIPTION  $\Rightarrow$  CLASS is not a discriminant rule of DB and write your own example for the dataset below.

**Given a dataset:**

Record	$a_1$	$a_2$	$a_3$	$a_4$	C
<b>o<sub>1</sub></b>	+	1	1	0	+
<b>o<sub>2</sub></b>	+	1	2	0	+
<b>o<sub>3</sub></b>	-	0	0	0	-
<b>o<sub>4</sub></b>	-	0	2	1	-
<b>o<sub>5</sub></b>	+	1	1	0	+

C – class attribute

**Q2.** Use the data set given above to create an example of a characteristic rule  $\text{CLASS} \Rightarrow \text{DESCRIPTION}$  such that the corresponding formula  $\text{DESCRIPTION} \Rightarrow \text{CLASS}$  is not a discriminant rule.

**Q3.** For the data set given above find  $\{o : \text{DESCRIPTION}\}$  for the following descriptions

- 1)  $a_1 = + \wedge a_2 = 1$
- 2)  $a_3 = 1 \wedge a_4 = 0$
- 3)  $a_2 = 0 \wedge a_1 = +$
- 4)  $a_1 = \{o : C = +\}, \{o : C = -\}$

**Q4.** For the following formulae determine whether they are / are not DISCRIMINANT / CHARACTERISTIC RULES of our dataset.

- 1)  $a_1 = + \wedge a_2 = 1 \Rightarrow C = -$
- 2)  $C = + \Rightarrow a_1 = - \wedge a_2 = 1 \wedge a_3 = 1$
- 3)  $C = - \Rightarrow a_1 = 1$
- 4)  $C = + \Rightarrow a_1 = + \wedge a_4 = 0$
- 5)  $a_1 = + \wedge a_2 = 1 \wedge a_3 = 1 \Rightarrow C = +$
- 6)  $a_1 = + \wedge a_3 = 2 \Rightarrow C = -$

## PART FOUR – Classification by Decision Tree Induction I

Given a TRAINING and TEST classification data as follows:

TRAINING

Record	$a_1$	$a_2$	$a_3$	C
<b>o<sub>1</sub></b>	1	1	0	+
<b>o<sub>2</sub></b>	0	0	1	-
<b>o<sub>3</sub></b>	0	1	1	+
<b>o<sub>4</sub></b>	0	0	1	-
<b>o<sub>5</sub></b>	1	1	0	+
<b>o<sub>6</sub></b>	1	1	1	-
<b>o<sub>7</sub></b>	0	0	0	-
<b>o<sub>8</sub></b>	0	0	1	-

TEST

Record	$a_1$	$a_2$	$a_3$	C
<b>o<sub>1</sub></b>	1	1	0	+
<b>o<sub>2</sub></b>	1	0	1	-
<b>o<sub>3</sub></b>	0	0	1	+
<b>o<sub>4</sub></b>	0	0	0	-

**Q1.** Use attribute  $a_2$  as the ROOT of the Decision Tree. Construct the tree (show steps) using your own choice of all node attributes.

**Q2.** Write down all the discriminant rules determined by your tree in two forms:

1. using the  $att = v$  expression and in a PREDICATE form using expressions
2.  $att(x, v)$  instead of  $att = v$ .
3. Are all of the rules determined by your tree TRUE in the TRAINING SET?

**Q3.** Use the TEST data to evaluate predictive accuracy of your set of rules generated by the given TRAINING data.

**Q4.** Re-write your TEST data using your choice of “real” values for attributes and values instead of our “abstract” attributes values.

Example             $a_1 = \text{age}, \quad 1 = \text{old}, \quad 0 = \text{young}$   
                           $a_2 = \text{color}, \quad 1 = \text{blue}, \quad 0 = \text{red}$

## **PART FIVE – ID3 Algorithm for DECISION TREE**

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**Q1.** For the data set given below, split it into TRAIN and TEST using not repeated Holdout ( $N - N/3 ; N/3$ ).

**Q2.** Construct the Decision Tree using ID3 algorithm using your own choice of attributes as consecutive nodes.

**Q3.** Construct the Decision Tree using ID3 algorithm with the General Majority Voting (i.e. majority voting at any node of the tree) using your own choice of attributes as consecutive nodes.

**Q4.** Write down the set of discovered DISCRIMINANT RULES for Q2 and Q3. Evaluate accuracy of your rules.

**Q5.** Evaluate predictive accuracy for your both sets of rules from Q4 and your choice of the TEST data.

CLASSIFICATION DATA:

Age	Income	Student	Credit Rating	Buys Computer
<=30	high	yes	Fair	No
<=30	high	No	Excellent	No
31...40	high	No	Fair	Yes
>40	medium	yes	Fair	Yes
>40	Low	no	Fair	Yes
>40	low	Yes	Excellent	No
31...40	low	Yes	Excellent	No
<=30	medium	Yes	Fair	No
>40	high	Yes	Fair	No
>40	low	Yes	Fair	No
<=30	medium	Yes	Excellent	Yes
>40	medium	No	Excellent	Yes
31...40	high	Yes	Fair	No
>40	medium	No	Excellent	No

## **PART SIX – Neural Networks Classification**

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Given two records (Training Sample)

$a_1$	$a_2$	$a_3$	Class
0.5	0	0.2	1
0.1	0.3	0.2	1
-0.1	0.2	-0.3,	0
-0.2	0.1	-0.1	0

1. Construct a Neural Network with one hidden layer (your own topology) and evaluate a passage of TWO EPOCHS.

**Use Learning Rate  $\ell = 0.7$**

REMEMBER: YOU HAVE TO SET YOUR INITIAL WEIGHTS AND BIASES RANDOMLY;

2. Write you're the terminating conditions for your network
3. Write a condition for success; i.e. how you decide that the record is well classified.