

Introduction to Medical Imaging

X-Ray Computed Tomography

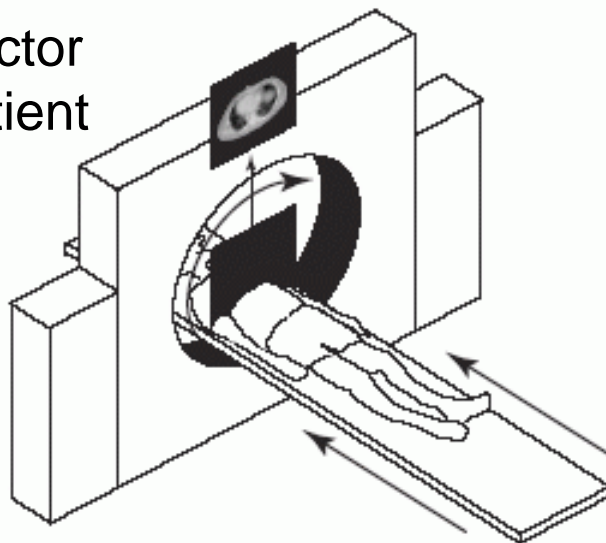
Klaus Mueller

Computer Science Department

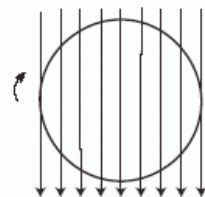
Stony Brook University

Overview

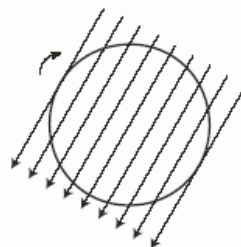
Scanning:
rotate source-detector
pair around the patient



reconstructed cross-sectional slice



reconstruction routine

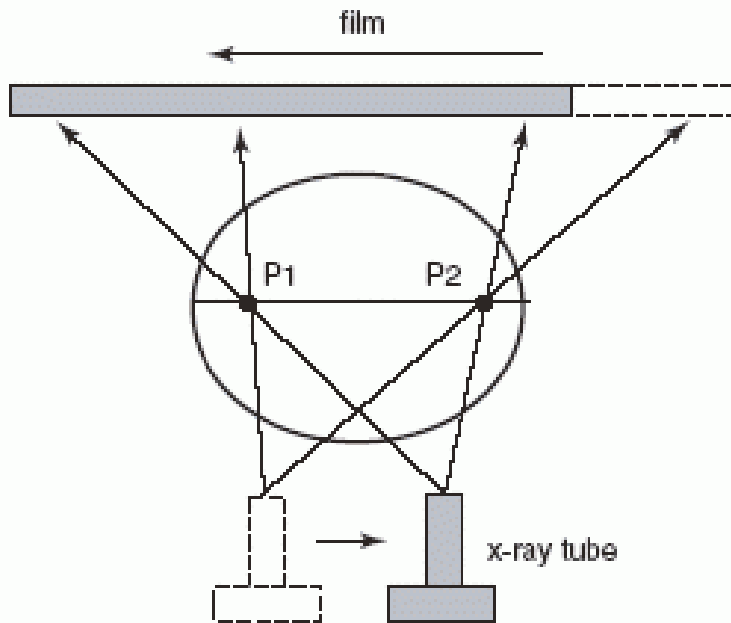


data

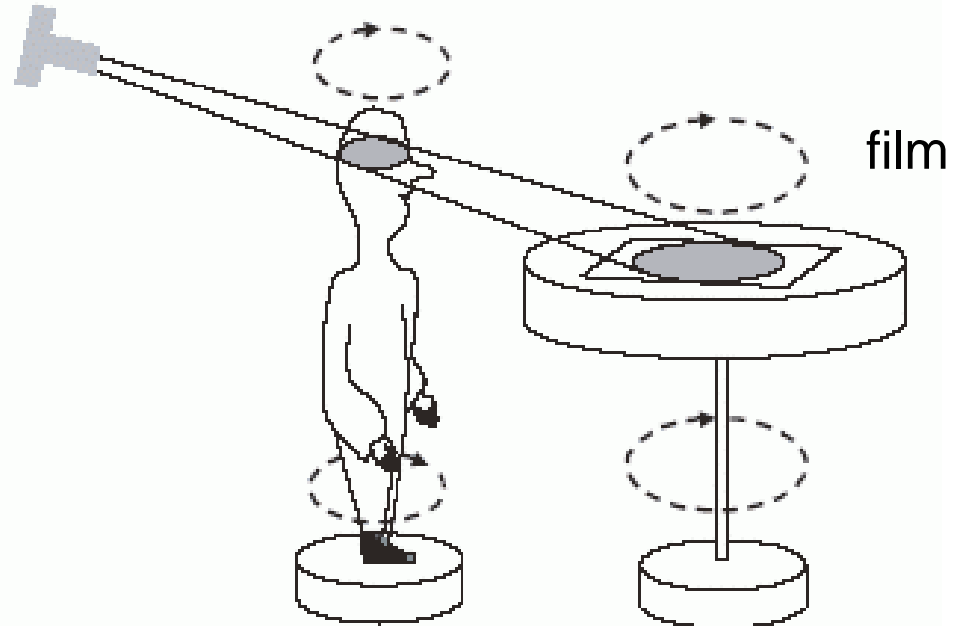


sinogram: a line for every angle

Early Beginnings



Linear tomography
only line P1-P2 stays in focus
all others appear blurred



Axial tomography
in principle, simulates the
backprojection procedure used in
current times

Current Technology

Principles derived by Godfrey Hounsfield for EMI

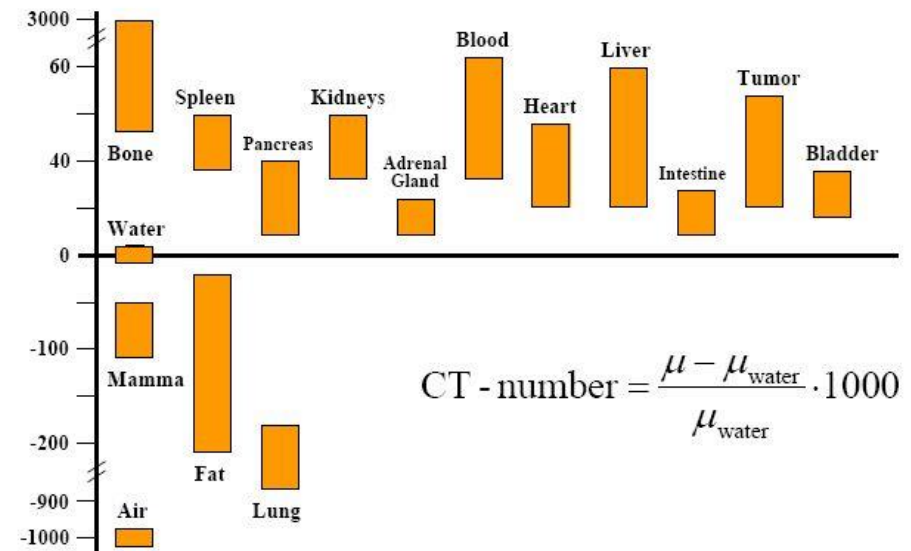
- based on mathematics by A. Cormack
- both received the Nobel Prize in medicine/physiology in 1979
- technology is advanced to this day



Images:

- size generally 512 x 512 pixels
- values in *Hounsfield units* (HU) in the range of -1000 to 1000

μ : linear attenuation coefficient



- due to large dynamic range, windowing must be used to view an image

CT Detectors

Scintillation crystal with photomultiplier tube (PMT)

(scintillator: material that converts ionizing radiation into pulses of light)

- high QE and response time
- low packing density
- PMT used only in the early CT scanners

Gas ionization chambers

- replace PMT
- X-rays cause ionization of gas molecules in chamber
- ionization results in free electrons/ions
- these drift to anode/cathode and yield a measurable electric signal
- lower QE and response time than PMT systems, but higher packing density

Scintillation crystals with photodiode

- current technology (based on solid state or semiconductors)
- photodiodes convert scintillations into measurable electric current
- QE > 98% and very fast response time

Projection Coordinate System

The parallel-beam geometry at angle θ represents a new coordinate system (r, s) in which projection $I_\theta(r)$ is acquired

- rotation matrix R transforms coordinate system (x, y) to (r, s) :

$$\begin{pmatrix} r \\ s \end{pmatrix} = R \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

that is, all (x, y) points that fulfill

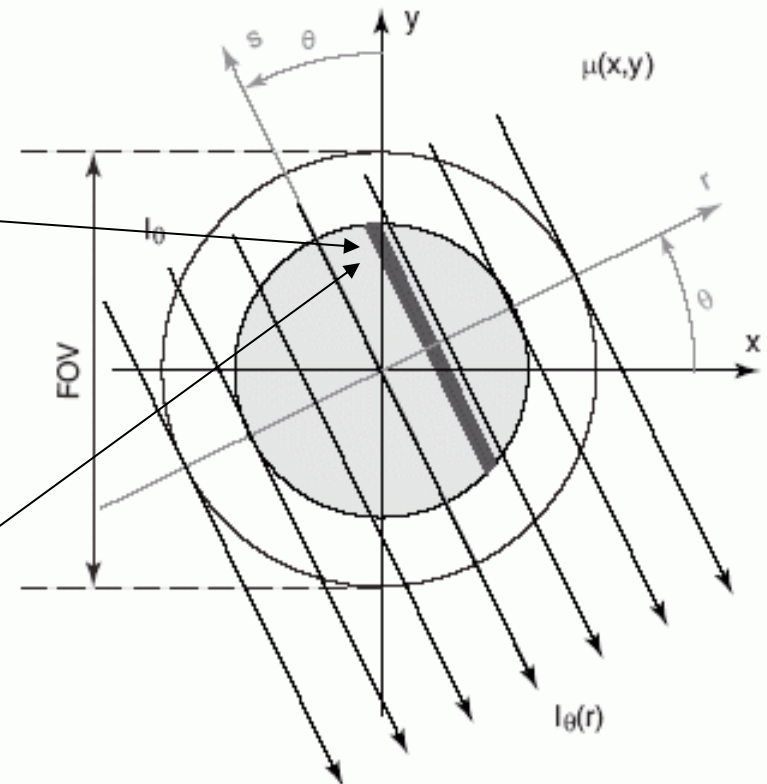
$$r = x \cos(\theta) + y \sin(\theta)$$

are on the (ray) line $L_{(r, \theta)}$

- R^T is the inverse, mapping (r, s) to (x, y)

$$\begin{pmatrix} x \\ y \end{pmatrix} = R^T \begin{pmatrix} r \\ s \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} r \\ s \end{pmatrix}$$

s is the parametric variable along the (ray) line $L_{(r, \theta)}$



Projection

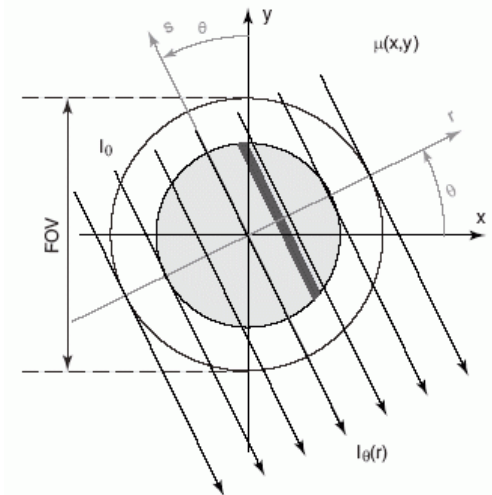
Assuming a fixed angle θ , the measured intensity at detector position r is the integrated density along $L_{(r,\theta)}$:

$$I_{\theta}(r) = I_0 \cdot e^{-\int \mu(x,y) ds}$$
$$= I_0 \cdot e^{-\int \mu(r \cdot \cos \theta - s \cdot \sin \theta, r \cdot \sin \theta + s \cdot \cos \theta) ds}$$

For a continuous energy spectrum:

$$I_{\theta}(r) = \int_0^{\infty} I_0(E) \cdot e^{-\int \mu(r \cdot \cos \theta - s \cdot \sin \theta, r \cdot \sin \theta + s \cdot \cos \theta) ds} dE$$

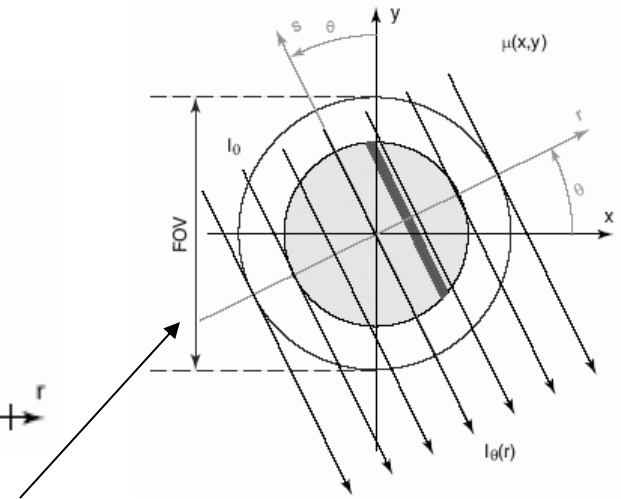
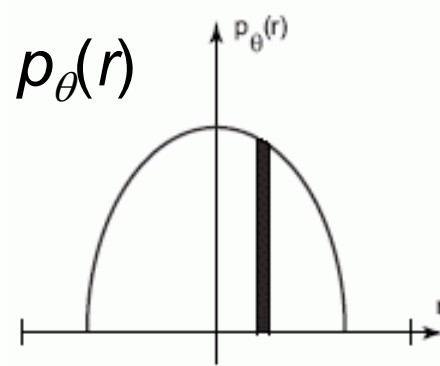
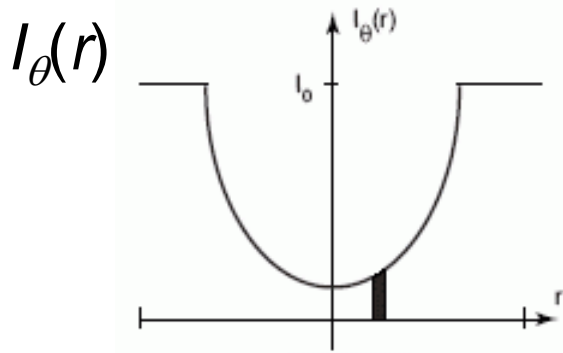
But in practice, it is assumed that the X-rays are monochromatic



Projection Profile

Each intensity profile $I_\theta(r)$ is transformed into an attenuation profile $p_\theta(r)$:

$$p_\theta(r) = -\ln \frac{I_\theta(r)}{I_0} = \int_{L_{r,\theta}} \mu(r \cdot \cos \theta - s \cdot \sin \theta, r \cdot \sin \theta + s \cdot \cos \theta) ds$$



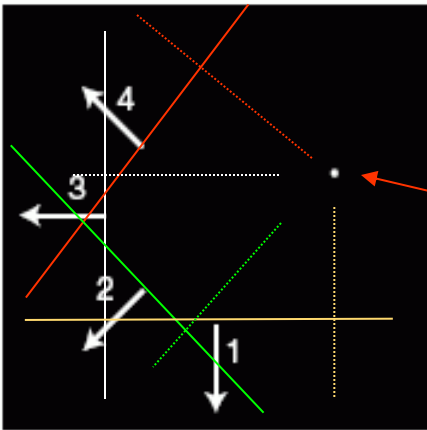
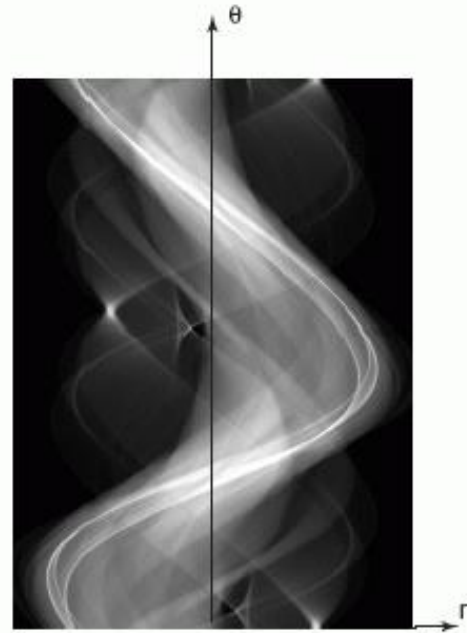
- $p_\theta(r)$ is zero for $|r| > FOV/2$ ($FOV =$ Field of View, detector width)
- $p_\theta(r)$ can be measured from $(0, 2\pi)$
- however, for parallel beam views $(\pi, 2\pi)$ are redundant, so just need to measure from $(0, \pi)$

Sinogram

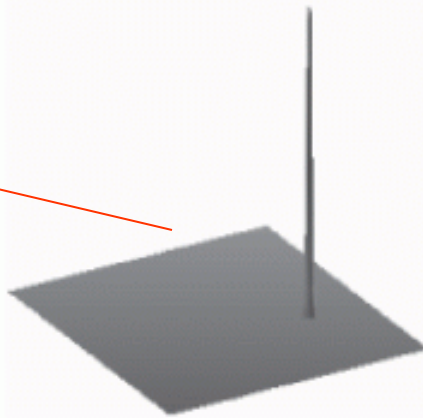
Stacking all projections (line integrals) yields the *sinogram*, a 2D dataset $p(r, \theta)$

To illustrate, imagine an object that is a single point:

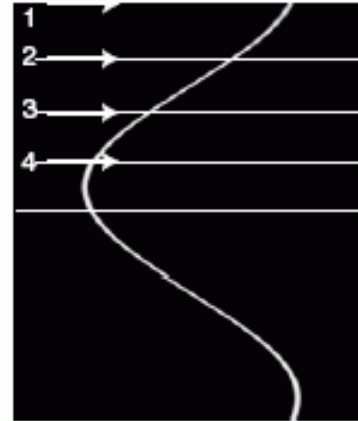
- it then describes a sinusoid in $p(r, \theta)$:



projections



point object



sinogram

Radon Transform

The transformation of any function $f(x,y)$ into $p(r,\theta)$ is called the *Radon Transform*

$$\begin{aligned} p(r,\theta) &= R\{f(x,y)\} \\ &= \int_{-\infty}^{\infty} f(r \cdot \cos \theta - s \cdot \sin \theta, r \cdot \sin \theta + s \cdot \cos \theta) ds \end{aligned}$$

The Radon transform has the following properties:

- $p(r,\theta)$ is periodic in θ with period 2π

$$p(r,\theta) = p(r,\theta + 2\pi)$$

- $p(r,\theta)$ is symmetric in θ with period π

$$p(r,\theta) = p(-r,\theta \pm \pi)$$

Sampling (1)

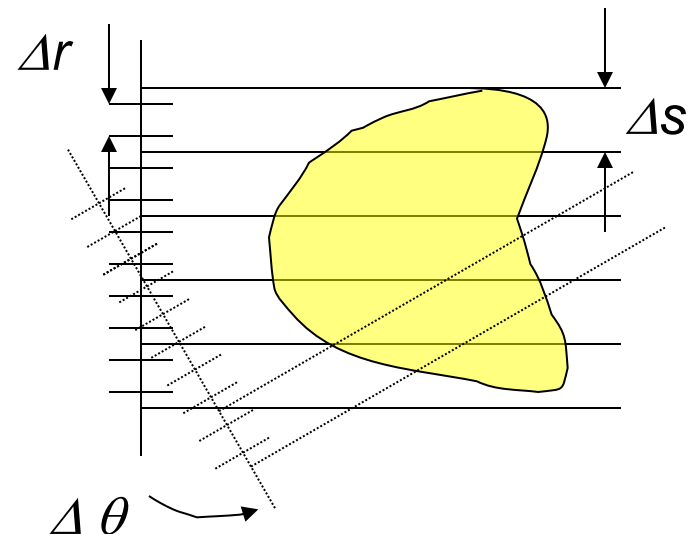
In practice, we only have a limited

- number of views, M
- number of detector samples, N
- for example, $M=1056$, $N=768$

This gives rise to a discrete sinogram $p(n\Delta r, m\Delta\theta)$

- a matrix with M rows and N columns
 Δr is the detector sampling distance
 $\Delta\theta$ is the rotation interval between subsequent views
- assume also a beam of width Δs

Sampling theory will tell us how to choose these parameters for a given desired object resolution



Sampling (2)

projection $p_{\theta}(r)$

*

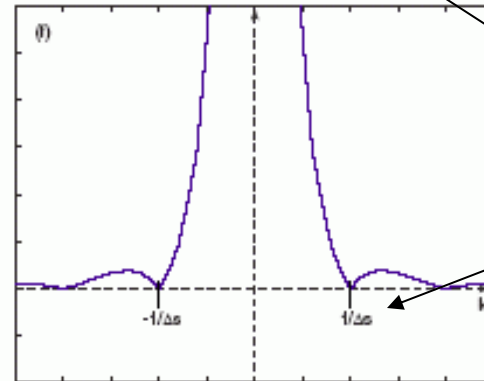
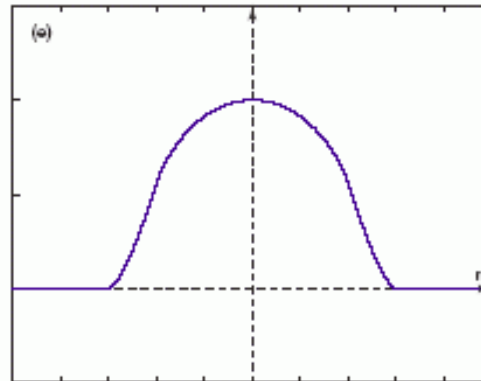
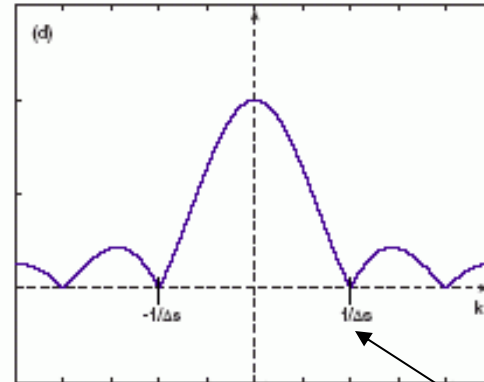
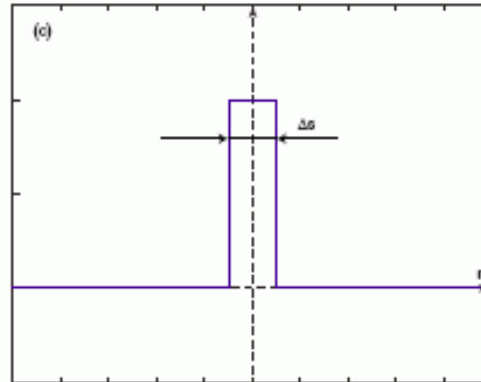
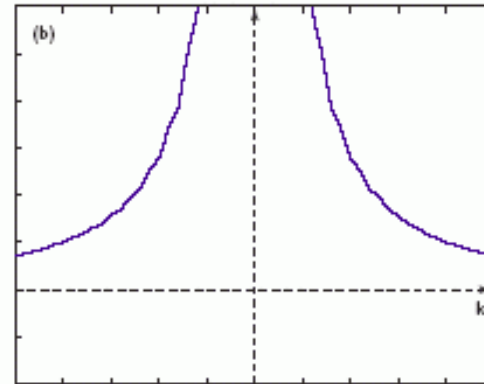
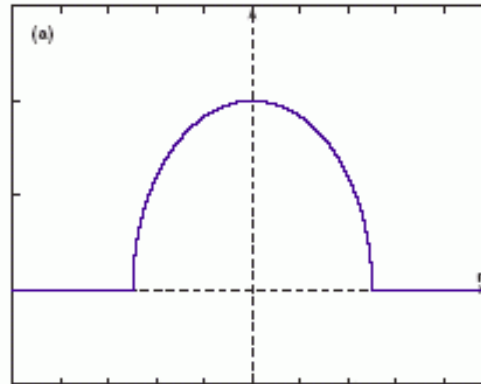
beam aperture Δs



smoothed projection

spatial domain

frequency domain



sinc function

$1 / \Delta s$

Sampling (3)

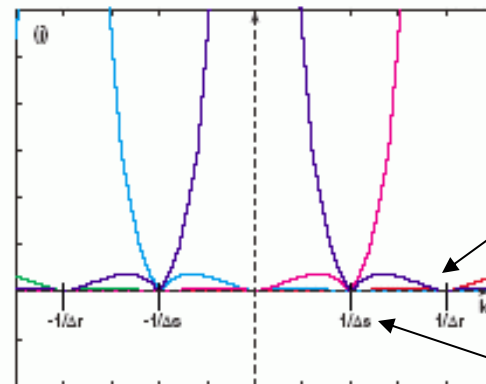
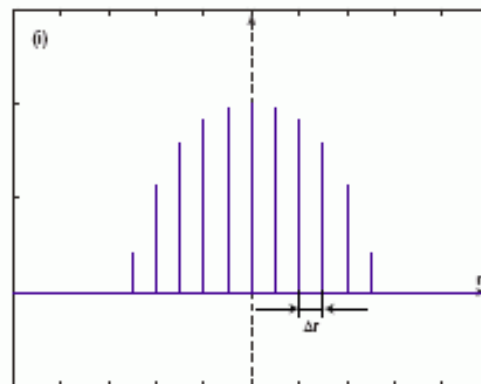
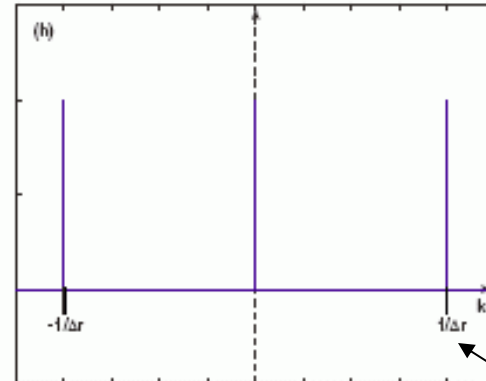
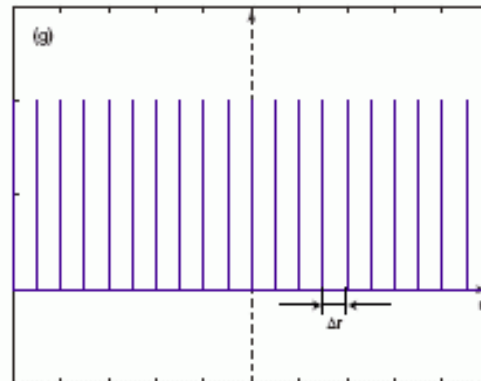
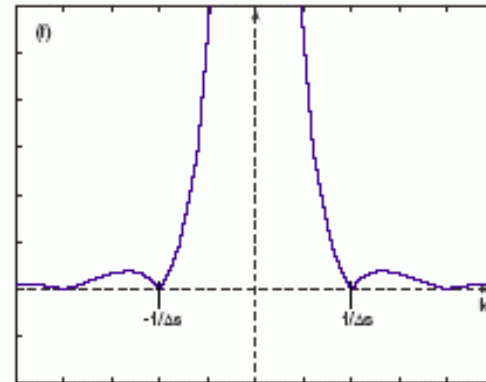
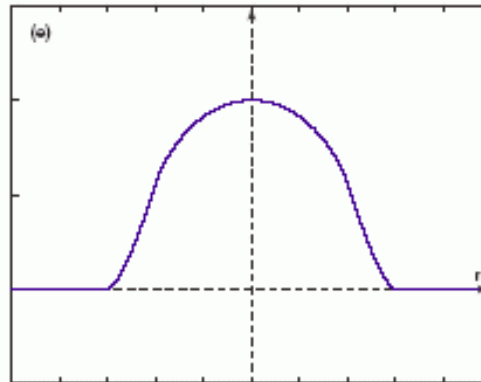
smoothed projection

•
sampling at Δr

↓
sampled projection

spatial domain

frequency domain



$1 / \Delta r$

$1 / \Delta s$

Limiting Aliasing

Aliasing within the sinogram lines (projection aliasing):

- to limit aliasing, we must separate the aliases in the frequency domain (at least coinciding the zero-crossings):

$$\frac{1}{\Delta r} \geq \frac{2}{\Delta s} \rightarrow \Delta r \leq \frac{\Delta s}{2}$$

- thus, at least 2 samples per beam are required

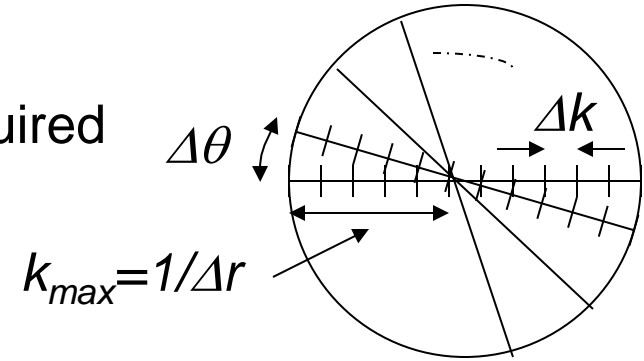
Aliasing across the sinogram lines (angular aliasing):

$$\Delta \theta = \frac{\pi k_{\max}}{M}$$

M : number of views, evenly distributed around the semi-circle

$$\Delta k = \frac{k_{\max}}{N/2}$$

N : number of detector samples, give rise to N frequency domain samples for each projection



sinogram in the frequency domain

(2 projections with $N=12$ samples each are shown)

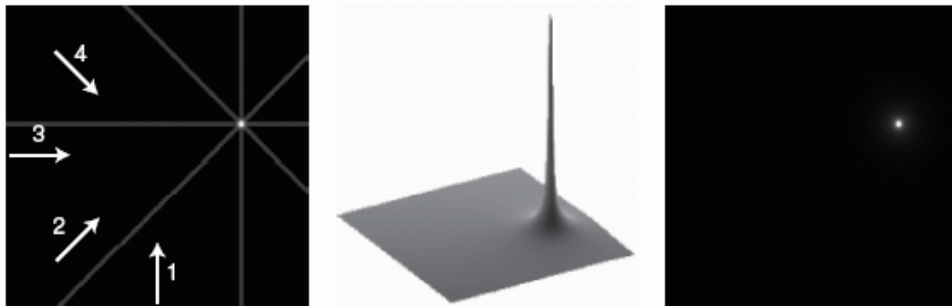
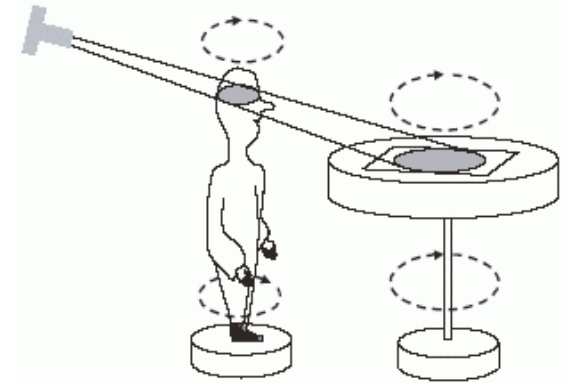
for uniform sampling: $\Delta \theta = \Delta k \rightarrow \frac{\pi k_{\max}}{M} = \frac{k_{\max}}{N/2} \rightarrow M = \pi \frac{N}{2}$

Reconstruction: Concept

Given the sinogram $p(r, \theta)$ we want to recover the object described in (x, y) coordinates

Recall the early axial tomography method

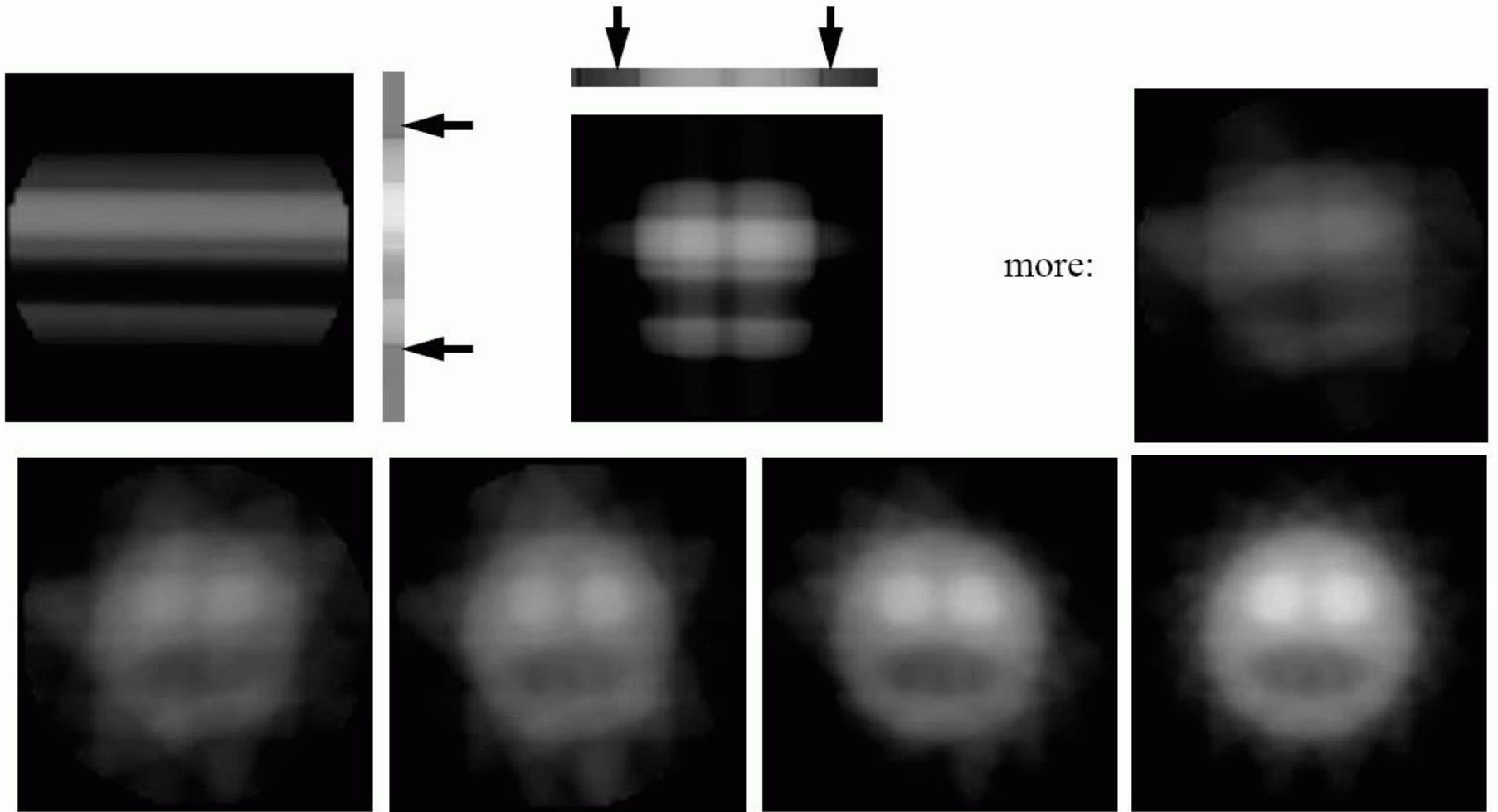
- basically it worked by subsequently “smearing” the acquired $p(r, \theta)$ across a film plate
- for a simple point we would get:



This is called *backprojection*:

$$b(x, y) = B\{p(r, \theta)\} = \int_0^{\pi} p(x \cdot \cos \theta + y \cdot \sin \theta, \theta) d\theta$$

Backprojection: Illustration



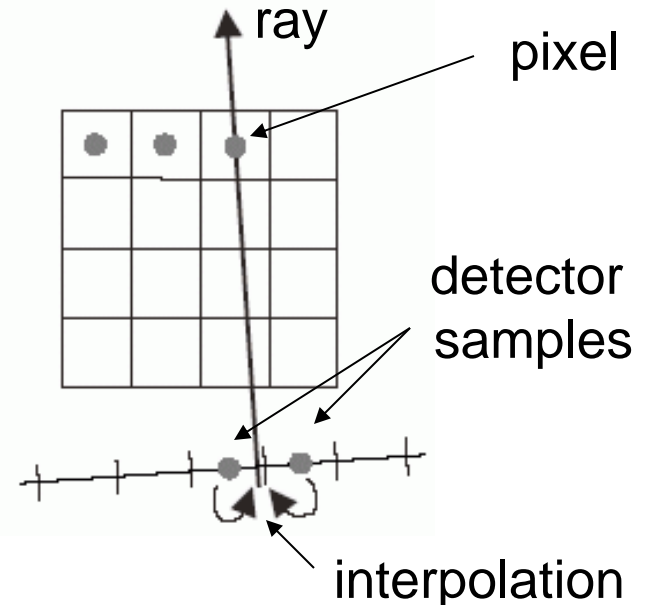
Backprojection: Practical Considerations

A few issues remain for practical use of this theory:

- we only have a finite set of M projections and a discrete array of N pixels (x_i, y_j)

$$b(x_i, y_j) = B\{p(r_n, \theta_m)\} = \sum_{m=1}^M p(x_i \cdot \cos \theta_m + y_j \cdot \sin \theta_m, \theta_m)$$

- to reconstruct a pixel (x_i, y_j) there may not be a ray $p(r_n, \theta_n)$ (detector sample) in the projection set
→ this requires interpolation (usually linear interpolation is used)

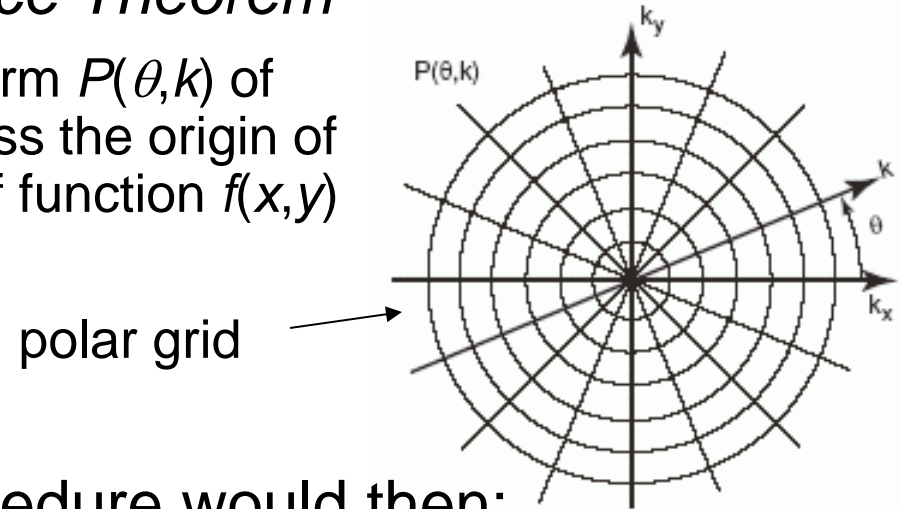


- the reconstructions obtained with the simple backprojection appear blurred (see previous slides)

The Fourier Slice Theorem

To understand the blurring we need more theory → the *Fourier Slice Theorem* or *Central Slice Theorem*

- it states that the Fourier transform $P(\theta, k)$ of a projection $p(r, \theta)$ is a line across the origin of the Fourier transform $F(k_x, k_y)$ of function $f(x, y)$

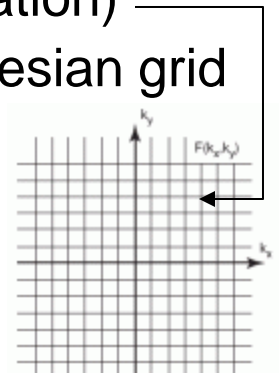


A possible reconstruction procedure would then:

- calculate the 1D FT of all projections $p(r_m, \theta_m)$, which gives rise to $F(k_x, k_y)$ sampled on a polar grid (see figure)
- resample the polar grid into a cartesian grid (using interpolation)
- perform inverse 2D FT to obtain the desired $f(x, y)$ on a cartesian grid

However, there are two important observations:

- interpolation in the frequency domain leads to artifacts
- at the FT periphery the spectrum is only sparsely sampled



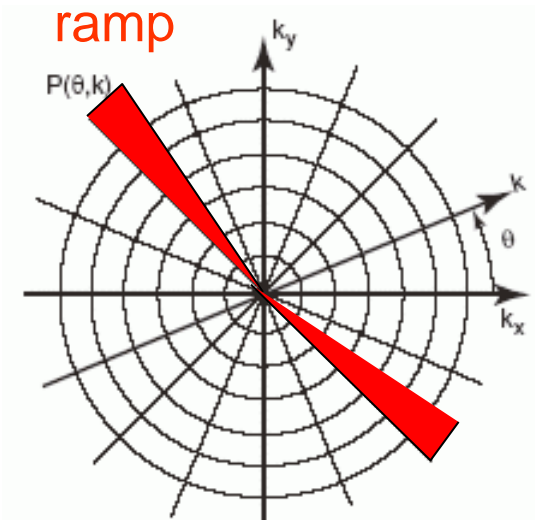
Filtered Backprojection: Concept

To account for the implications of these two observations, we modify the reconstruction procedure as follows:

- filter the projections to compensate for the blurring
- perform the interpolation in the spatial domain via backprojection
→ hence the name *Filtered Backprojection*

Filtering -- what follows is a more practical explanation (for formal proof see the book):

- we need a way to equalize the contributions of all frequencies in the FT's polar grid
- this can be done by multiplying each $P(\theta, k)$ by a ramp function → this way the magnitudes of the existing higher-frequency samples in each projection are scaled up to compensate for their lower amount
- the ramp is the appropriate scaling function since the sample density decreases linearly towards the FT's periphery



Filtered Backprojection: Equation and Result

1D Fourier transform of $p(r, \theta)$
 $\rightarrow P(k, \theta)$

$$f(x, y) = \int_0^{\pi} \left(\int_{-\infty}^{\infty} P(k, \theta) \cdot |k| \cdot e^{i2\pi kr} dk \right) d\theta$$

The equation is annotated with three colored boxes and arrows:

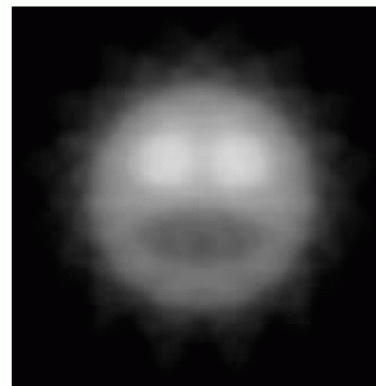
- A red box around the inner integral $\int_{-\infty}^{\infty} P(k, \theta) \cdot |k| \cdot e^{i2\pi kr} dk$ is labeled "ramp-filtering".
- A green box around the entire expression $\int_0^{\pi} \left(\int_{-\infty}^{\infty} P(k, \theta) \cdot |k| \cdot e^{i2\pi kr} dk \right) d\theta$ is labeled "inverse 1D Fourier transform $\rightarrow p(r, \theta)$ ".
- A blue box around the entire equation is labeled "backprojection for all angles".

backprojection for all angles

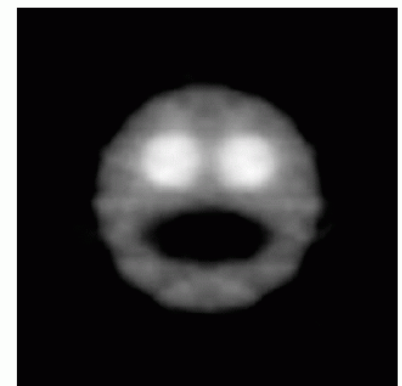
inverse 1D Fourier transform $\rightarrow p(r, \theta)$

Recall the previous (blurred) backprojection illustration

- now using the filtered projections:

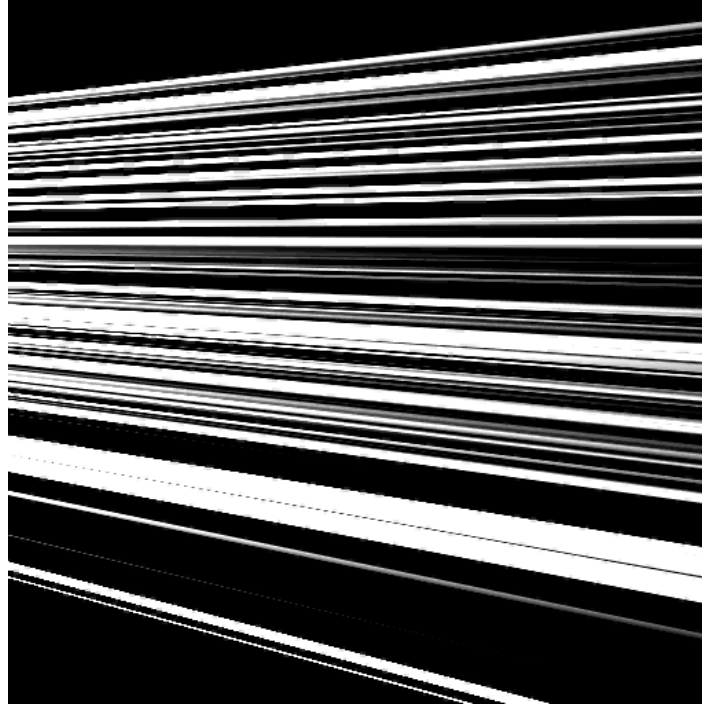


not filtered



filtered

Filtered Backprojection: Illustration



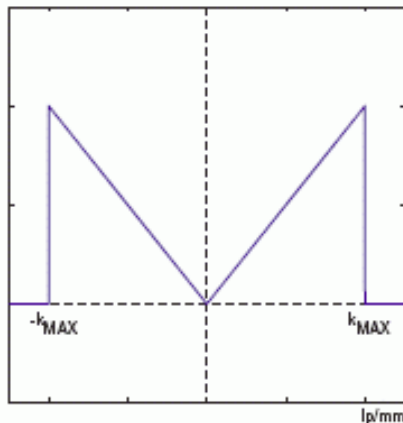
Filters

There are various filters (for formulas see the book) :

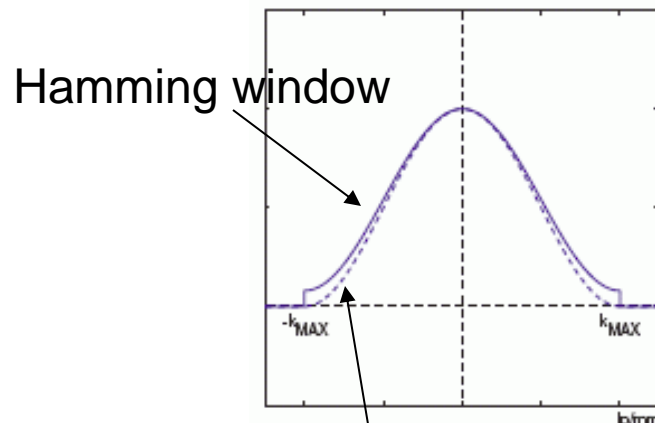
- all filters have large spatial extent \rightarrow convolution would be expensive
- therefore the filtering is usually done in the frequency domain \rightarrow the required two FT's plus the multiplication by the filter function has lower complexity

Popular filters (for formulas see book):

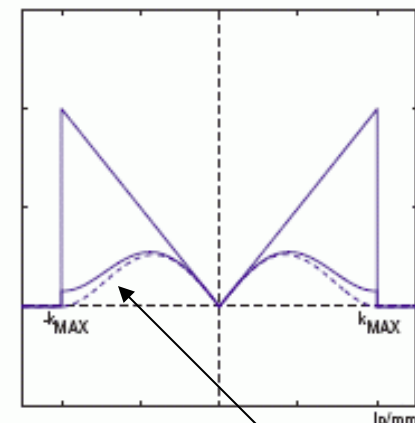
- Ram-Lak: original ramp filter limited to interval $[\pm k_{max}]$
- Ram-Lak with Hanning/Hamming smoothing window: de-emphasizes the higher spatial frequencies to reduce aliasing and noise



Ram-Lak



Hanning window



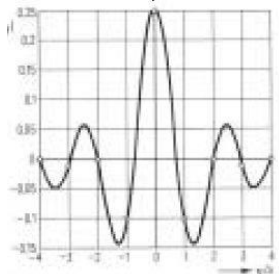
Windowed Ram-Lak

Filters (2)

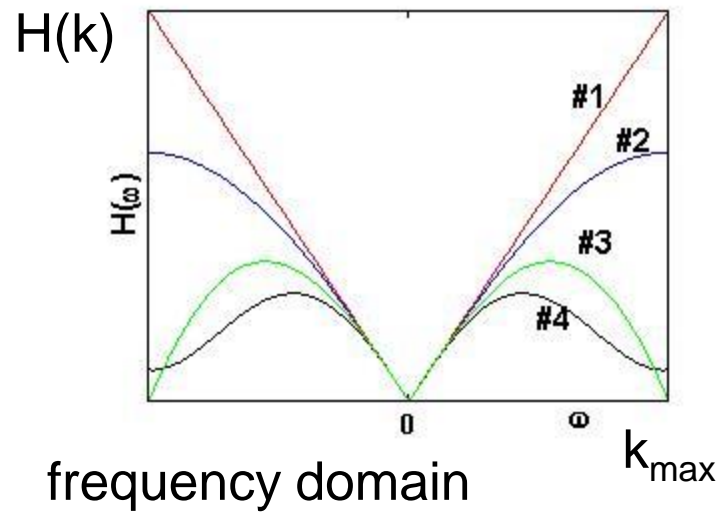
Frequency domain:

- #1: Ram-Lak

$$H(k) = |k|$$



spatial domain



frequency domain

- #2: Shepp-Logan

$$H(k) = |k| \cdot \text{sinc}\left(\frac{\pi k}{2k_{\max}}\right)$$

- #3: cosine $H(k) = \cos(k / k_{\max})$

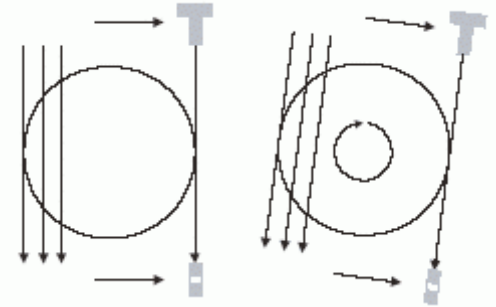
- #4: Hamming ($\alpha=0.54$) and Hanning ($\alpha=0.5$)

$$H(k) = \alpha + (1 - \alpha) \cos\left(\frac{\pi k}{k_{\max}}\right)$$

Beam Geometry

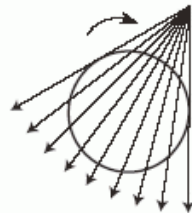
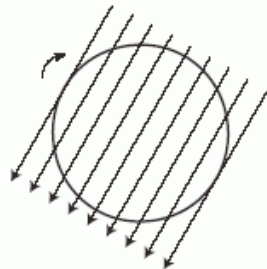
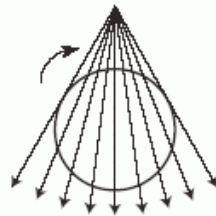
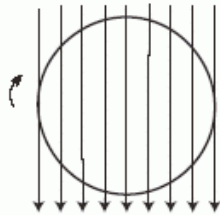
The parallel-beam configuration is not practical

- it requires a new source location for each ray



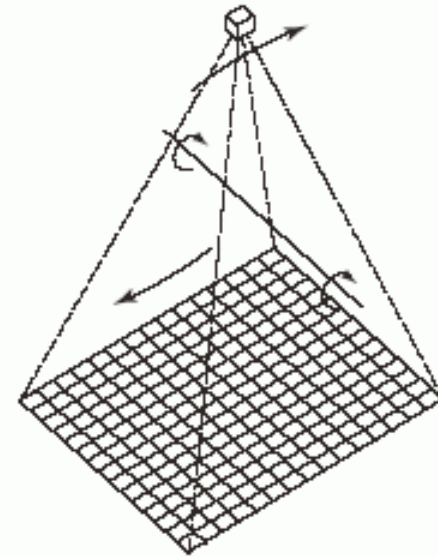
We'd rather get an image in "one shot"

- the requires *fan-beam* acquisition



parallel-beam

fan-beam



cone-beam in 3D

Fan-Beam Mathematics (1)

Rewrite the parallel-beam equations into the fan-beam geometry

Recall:

- filtering:

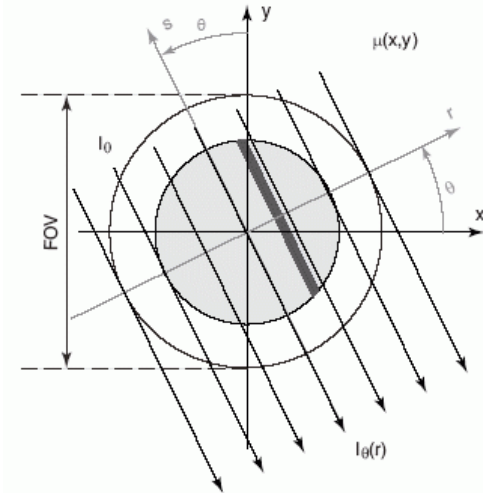
$$p^*(r, \theta) = \int_{-FOV/2}^{+FOV/2} p(r', \theta) q(r - r') dr'$$

- backprojection:

$$f(x, y) = \int_0^{\pi} p^*(r, \theta) d\theta \quad \text{with } r = x \cos \theta + y \sin \theta$$

- and combine:

$$f(x, y) = \int_0^{2\pi + FOV/2} \int_{-FOV/2}^{+FOV/2} p(r', \theta) q(x \cos \theta + y \sin \theta - r') dr' d\theta$$



Fan-Beam Mathematics

$$f(x, y) = \int_0^{2\pi + FOV/2} \int_{-FOV/2} p(r', \theta) q(x \cos \theta + y \sin \theta - r') dr' d\theta$$

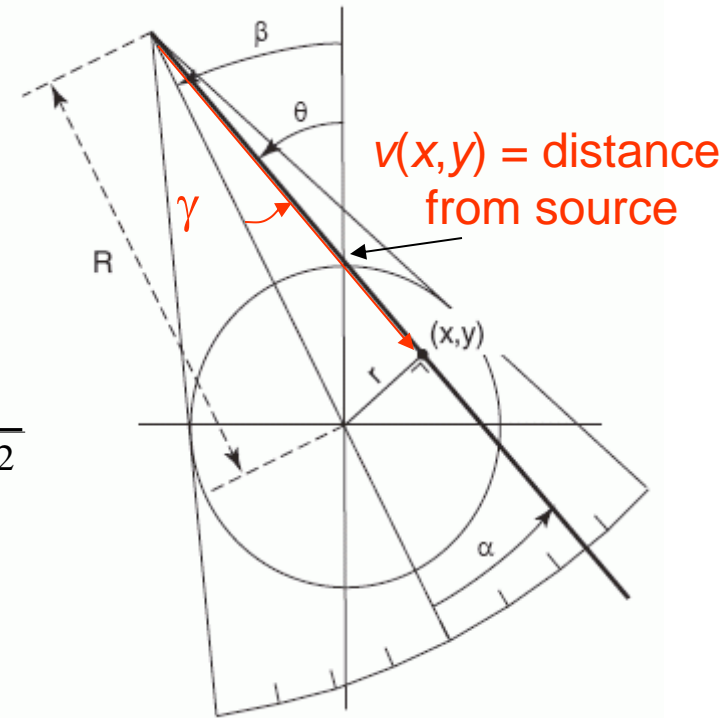
- with change of variables:

$$\theta = \alpha + \beta \quad r = R \sin \alpha$$

- for a voxel (x, y) : v = distance, γ = angle

$$v = \sqrt{(x \cos \beta + y \sin \alpha)^2 + (x \sin \beta - y \cos \alpha + R)^2}$$

$$\gamma = (x \cos \beta + y \sin \alpha) / (x \sin \beta - y \cos \alpha + R)$$



the projection at β

$$f(x, y) = \int_0^{2\pi} \frac{1}{v^2(x, y)} \int_{-fan-angle/2}^{+fan-angle/2} R \cos \alpha \cdot p(\alpha, \beta) \cdot \left(\frac{\gamma - \alpha}{2 \sin(\gamma - \alpha)} \right) q(\gamma - \alpha) d\alpha d\beta$$

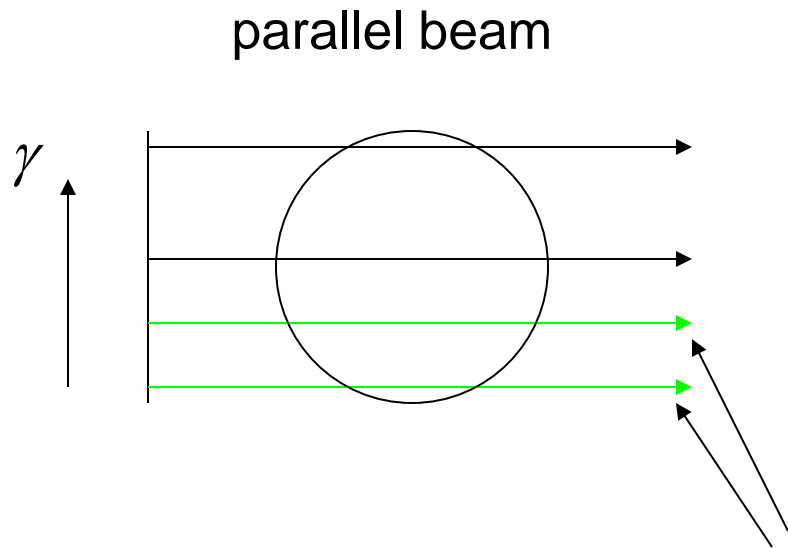
3. weighting during backprojection

1. projection pre-weighting

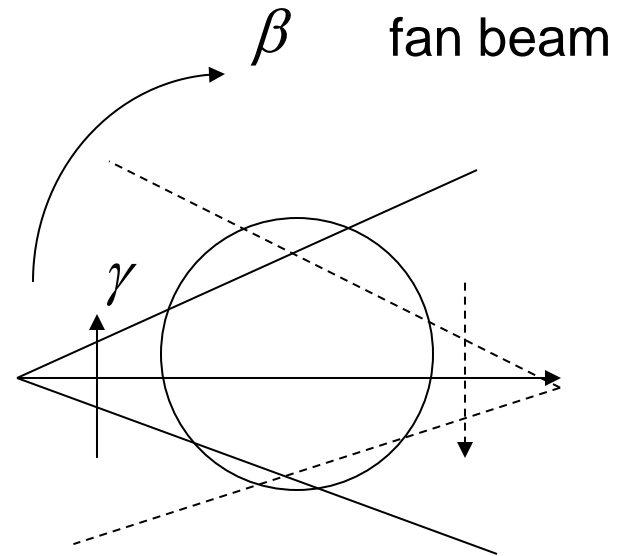
2. filter

Fan-Beam Mathematics

Problem: fan-beam does not fill the sinogram adequately

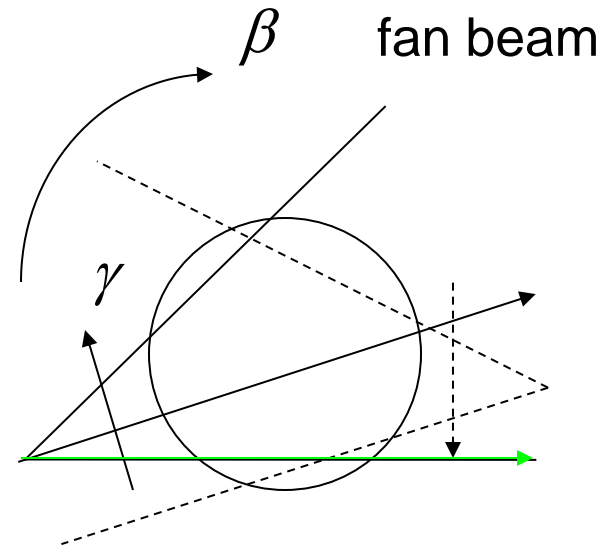
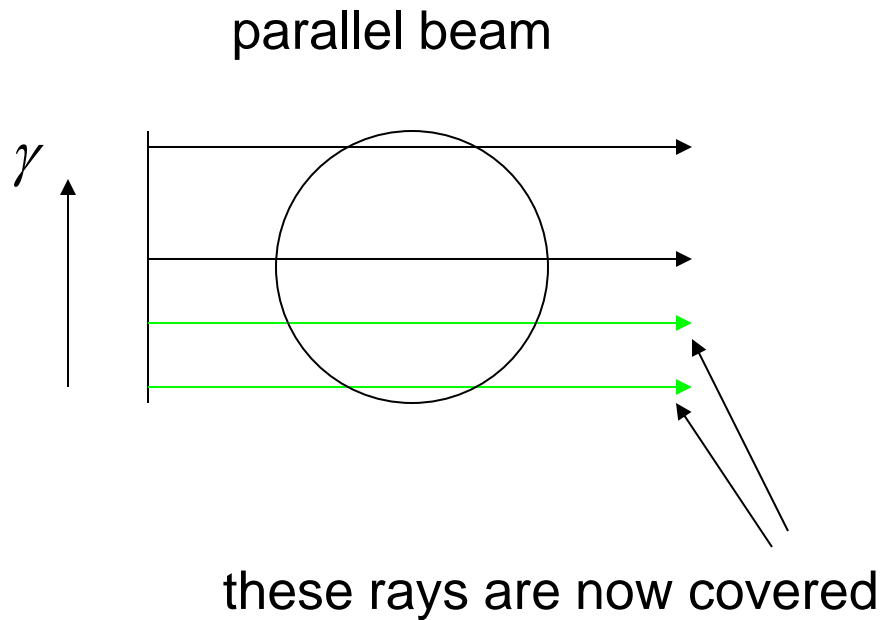


these rays (and others) are not covered by any fan-beam view



Fan-Beam Mathematics

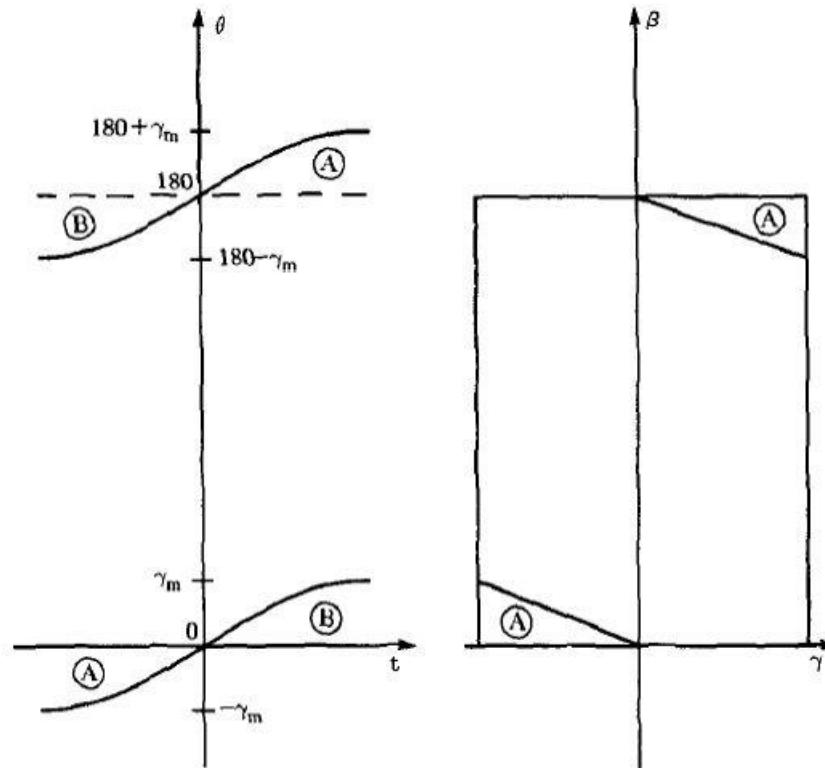
Solution: extend the source-detector trajectory by the fan half-angle on both ends



Fan-Beam Mathematics

More formally

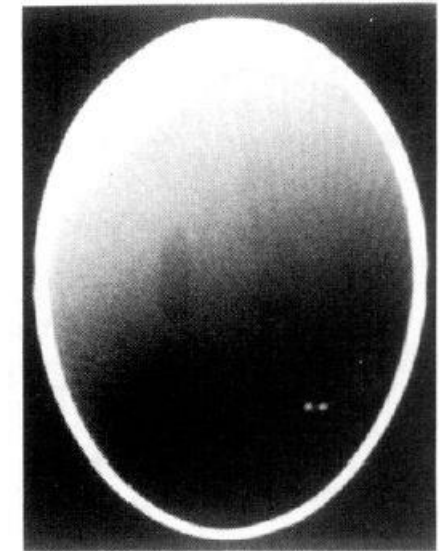
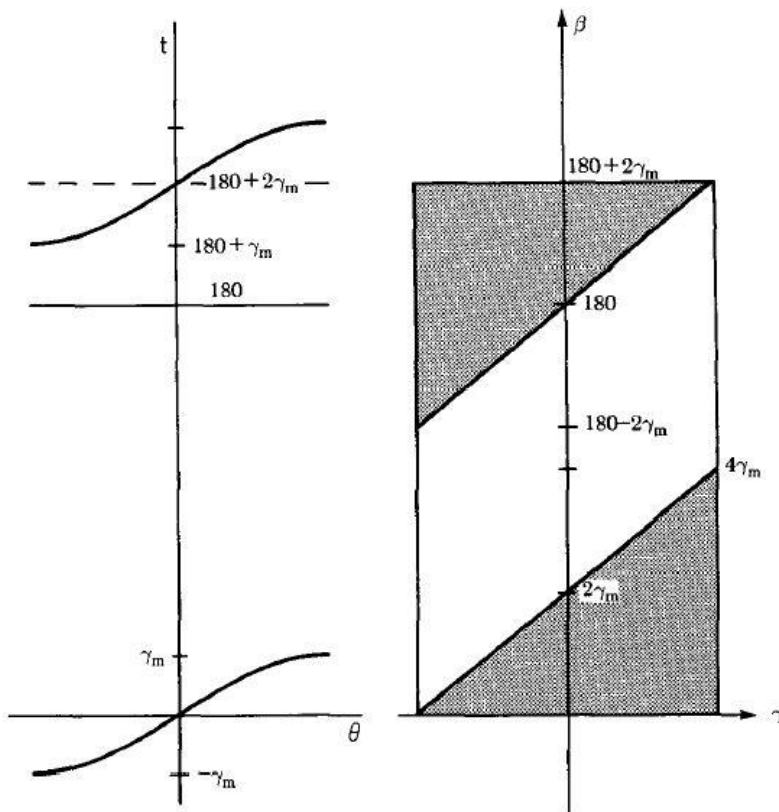
- region A is covered twice, while region B is not covered at all



Fan-Beam Mathematics

Extending the trajectory fills the space

- but some areas are filled twice, which causes problems



Fan-Beam Mathematics

Simply setting these regions to zero will result in heavy streak artifacts

- recall the filtering step?

Need to use a smoother window

- a smooth window is both continuous and has a continuous derivative at the boundary of single and double-overlap regions

$$\left. \frac{\partial w_{\beta}(\gamma)}{\partial \beta} \right|_{\beta=2\gamma_m+2\gamma} = 0$$

$$\left. \frac{\partial w_{\beta}(\gamma)}{\partial \beta} \right|_{\beta=180^{\circ}+2\gamma} = 0.$$

- the window weights for the same rays at opposite sides of the sinogram must be 1.

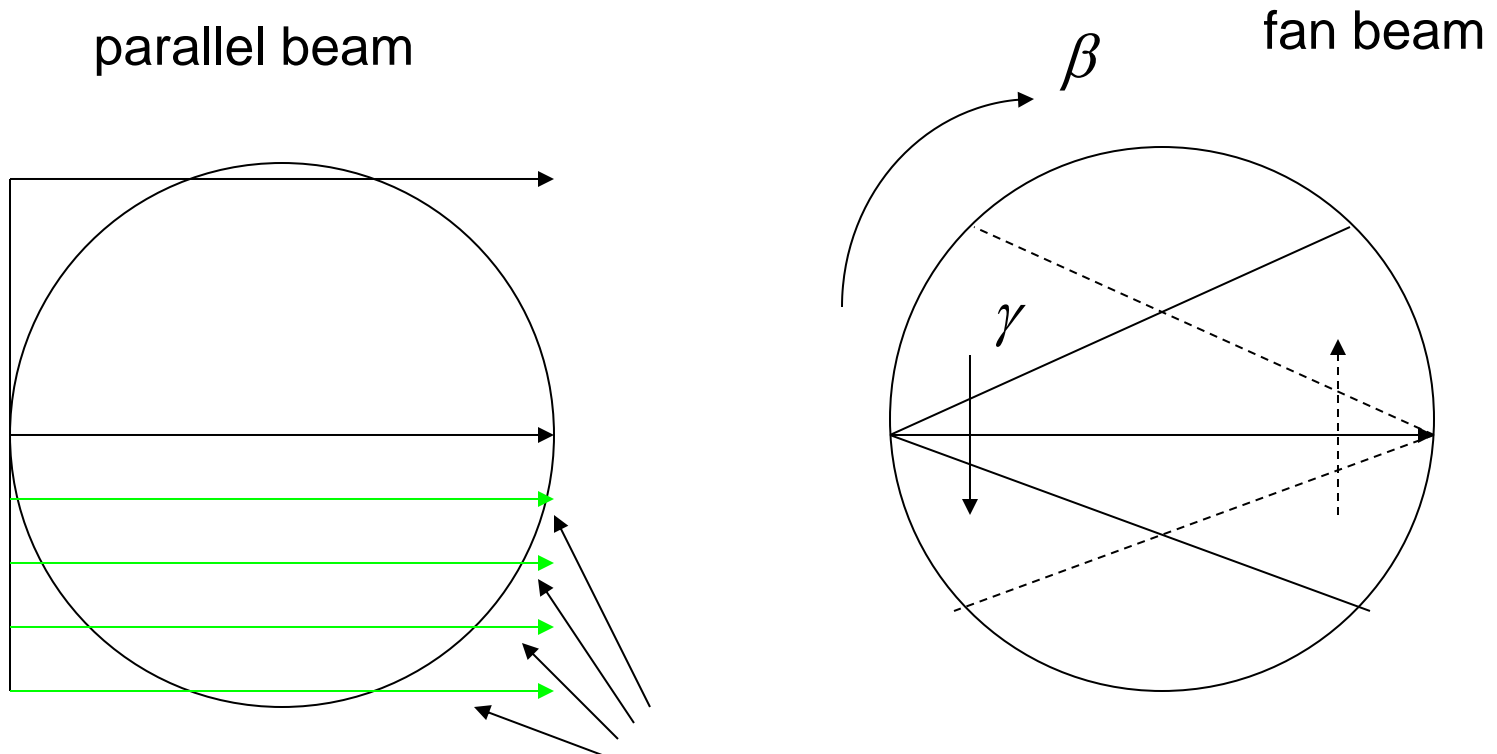
$$w_{\beta_1}(\gamma_1) + w_{\beta_2}(\gamma_2) = 1$$

- the Parker window fullfills these conditions: $w_{\beta}(\gamma) = \begin{cases} \sin^2 \left[\frac{45^{\circ} \beta}{\gamma_m - \gamma} \right], & 0 \leq \beta \leq 2\gamma_m - 2\gamma \\ 1, & 2\gamma_m - 2\gamma \leq \beta \leq 180^{\circ} - 2\gamma \\ \sin^2 \left[45^{\circ} \frac{180^{\circ} + 2\gamma_m - \beta}{\gamma + \gamma_m} \right], & 180^{\circ} - 2\gamma \leq \beta \leq 180^{\circ} + 2\gamma_m. \end{cases}$

Fan-Beam Mathematics (3)

See chapter in Kak-Slaney (posted on the class website) for equations associated with flat detectors

Compare with parallel beam sinogram fill



these rays (and others) are not covered by any fan-beam view

Remarks

In practice, need only fan-beam data in the angular range $[-\text{fan-angle}/2, 180^\circ + \text{fan-angle}/2]$

So, reconstruction from fan-beam data involves

- a pre-weighting of the projection data, depending on α
- a pre-weighting of the filter (here we used the spatial domain filters)
- a backprojection along the fan-beam rays (interpolation as usual)
- a weighting of the contributions at the reconstructed pixels, depending on their distance $v(x, y)$ from the source

Alternatively, one could also “rebin” the data into a parallel-beam configuration

- however, this requires an additional interpolation since there is no direct mapping into a uniform parallel-beam configuration

Lastly, there are also iterative algorithms

- these pose the reconstruction problem as a system of linear equations
- solution via iterative solves (more to come in the nuclear medicine lectures)

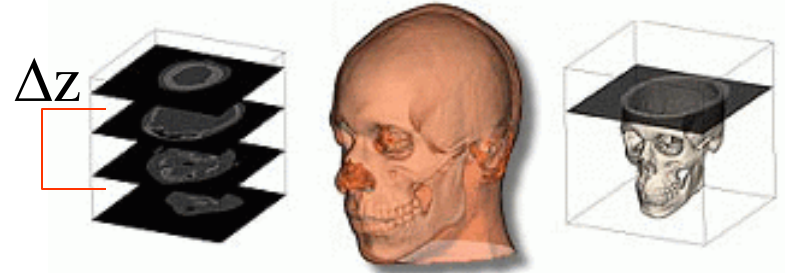
Fan-Beam Mathematics

See chapter in Kak-Slaney (posted on the class website) for equations associated with flat detectors

Imaging in Three Dimensions

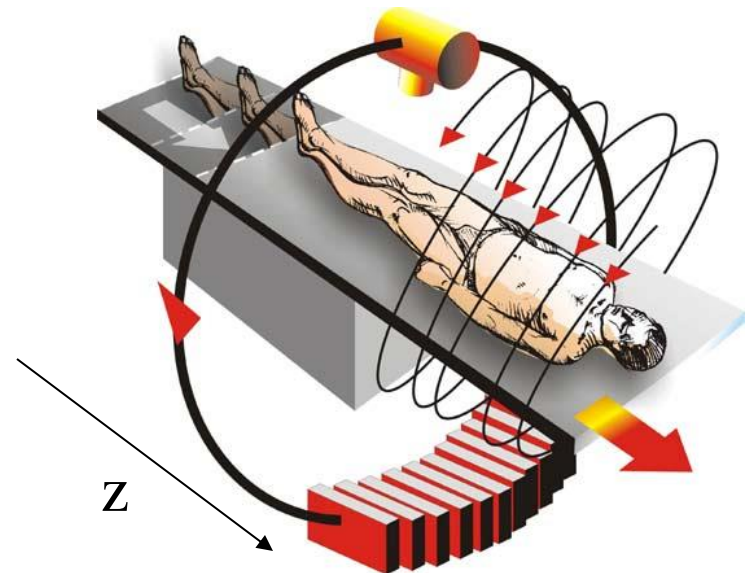
Sequential CT

- advance table with patient after each slice acquisition has been completed
- stop-motion is time consuming and also shakes the patient
- the *effective thickness* of a slice, Δz , is equivalent to the beam width Δs in 2D
- similarly: we must acquire 2 slices per Δz to combat aliasing



Spiral (helical) CT

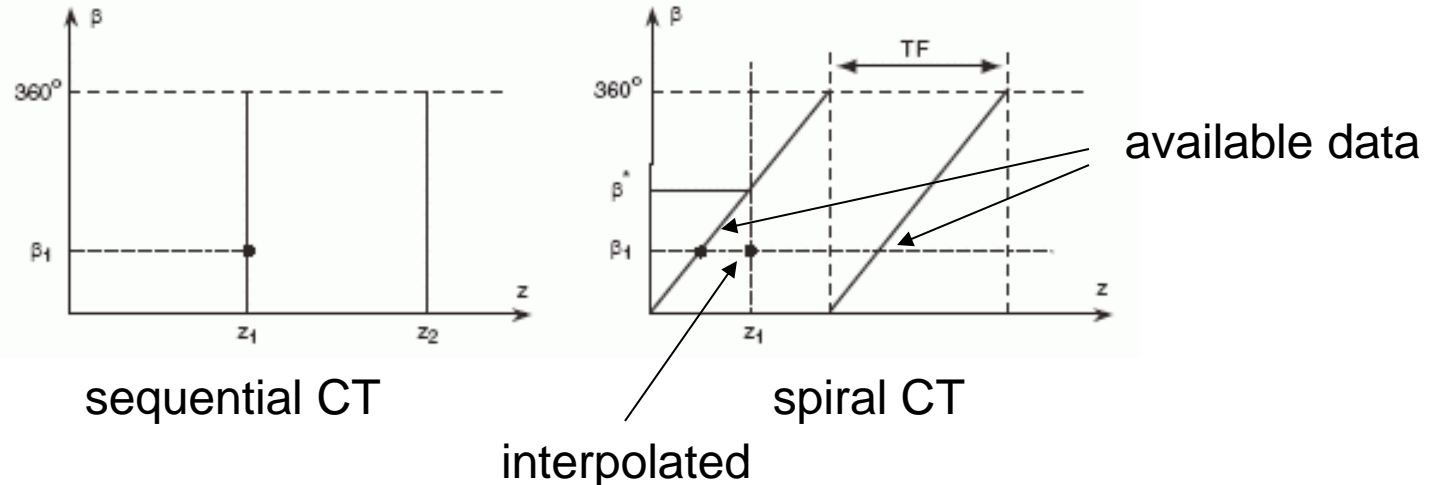
- table translates as tube rotates around the patient
- very popular technique
- fast and continuous
- *table feed (TF)* = axial translation per tube rotation
- *pitch* = $TF / \Delta z$



Reconstruction From Spiral CT Data

Note: the table is advancing (z grows) while the tube rotates (β grows)

- however, the reconstruction of a slice with constant z requires data from all angles β
- \rightarrow require some form of interpolation

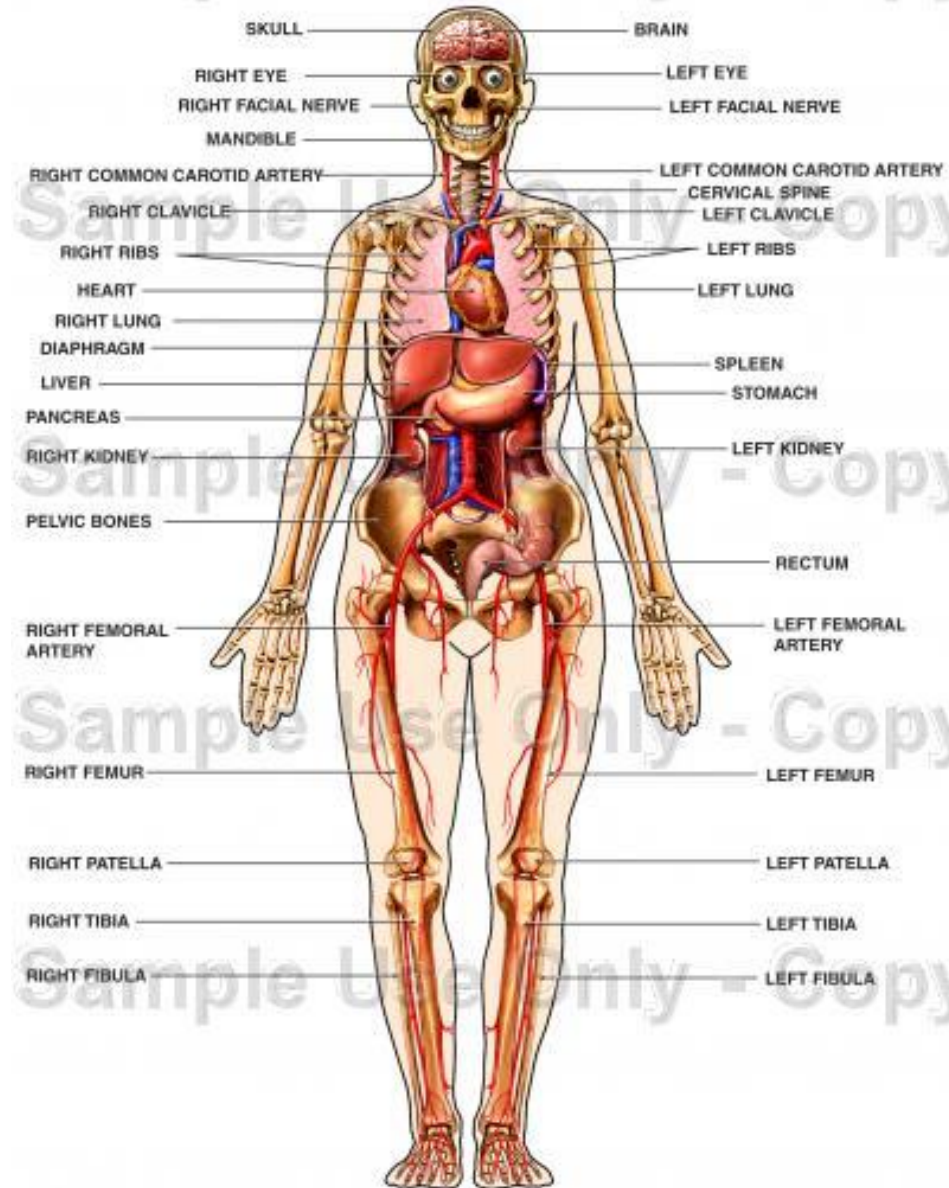


- if $TF = \Delta z / 2$ (see before), then a good pitch = $(\Delta z / 2) / \Delta z = 0.5$
- since opposing rays ($\beta = [180^\circ \dots 360^\circ]$) have (roughly) the same information, TF can double (and so can pitch = 1)
- in practice, pitch is typically between 1 and 2
- higher pitch lowers dose, scan-time, and reduces motion artifacts

Spiral CT Reconstruction



Human Anatomy - Anterior (Front) View ANTERIOR ANATOMY



3D Reconstruction From Cone-Beam Data

Most direct 3D scanning modality

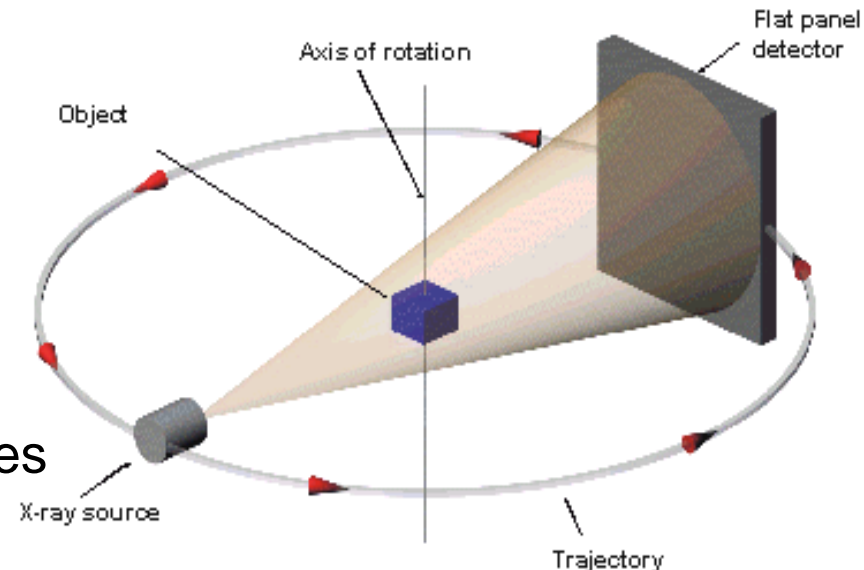
- uses a 2D detector
- requires only one rotation around the patient to obtain all data (within the limits of the cone angle)
- reconstruction formula can be derived in similar ways than the fan beam equation (uses various types of weightings as well)
- a popular equation is that by Feldkamp-Davis-Kress
- backprojection proceeds along cone-beam rays

Advantages

- potentially very fast (since only one rotation)
- often used for 3D angiography

Downsides

- sampling problems at the extremities
- reconstruction sampling rate varies along z



Factors Determining Image Quality

Acquisition

- focal spot, size of detector elements, table feed, interpolation method, sample distance, and others

Reconstruction

- reconstruction kernel (filter), interpolation process, voxel size

Noise

- quantum noise: due to statistical nature of X-rays
- increase of power reduces noise but increases dose
- image noise also dependent on reconstruction algorithm, interpolation filters, and interpolation methods
- greater Δz reduces noise, but lowers axial resolution

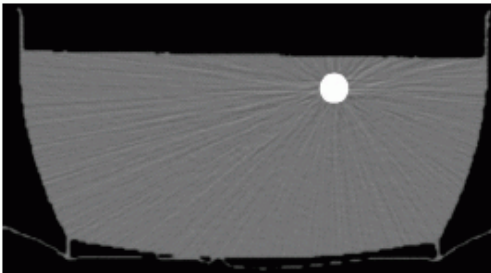
Contrast

- depends on a number of physical factors (X-ray spectrum, beam-hardening, scatter)

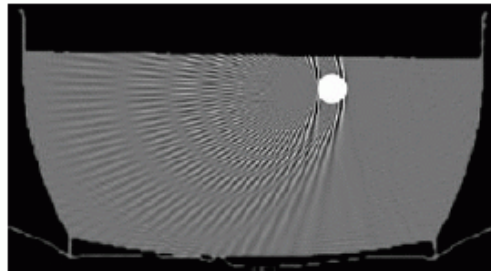
Image Artifacts (1)



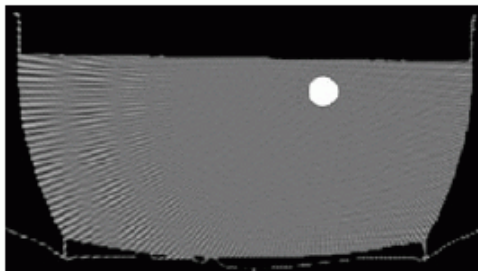
Normal phantom (simulated water with iron rod)



Adding noise to sinogram gives rise to streaks

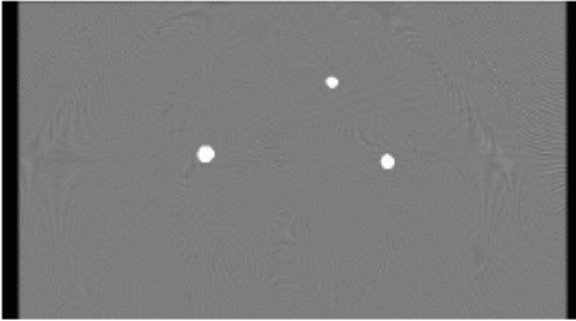


Aliasing artifacts when the number of samples is too small (ringing at sharp edges)

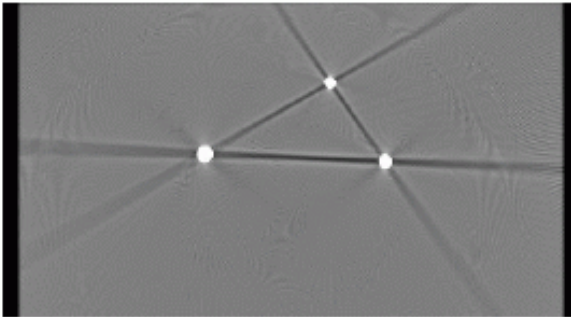


Aliasing artifacts when the number of views is too small

Image Artifacts (2)

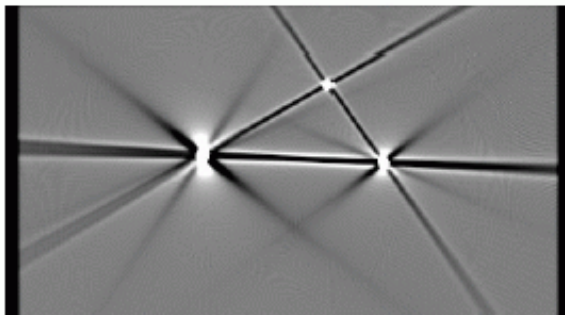


Normal phantom (plexiglas plate with three amalgam fillings)



Beam hardening artifacts

- non-linearities in the polychromatic beam attenuation (high opacities absorb too many low-energy photons and the high energy photons won't absorb)
- attenuation is under-estimated



Scatter (attenuation of beam is under-estimated)

- the larger the attenuation, the higher the percentage of scatter

Image Artifacts (3)

Partial volume artifact

- occurs when only part of the beam goes across an opaque structure and is attenuated
- most severe at sharp edges
- calculated attenuation: $-\ln(\text{avg}(I/I_0))$
- true attenuation: $-\text{avg}(\ln(I/I_0))$

$$-\ln(\text{avg}(I/I_0)) < -\text{avg}(\ln(I/I_0))$$

- will underestimate the attenuation

single pixel traversed
by individual rays:

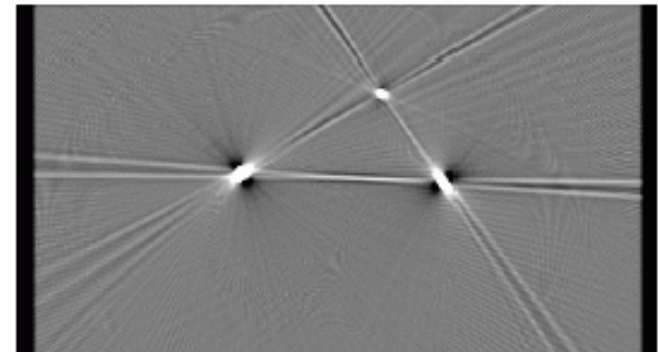
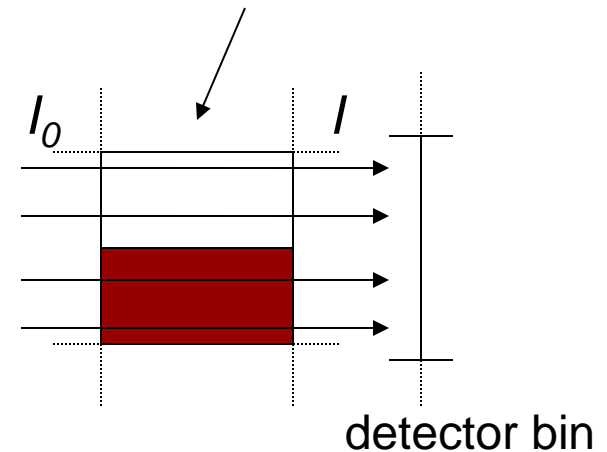
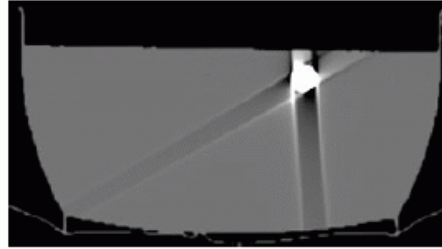


Image Artifacts (4)

Motion artifacts

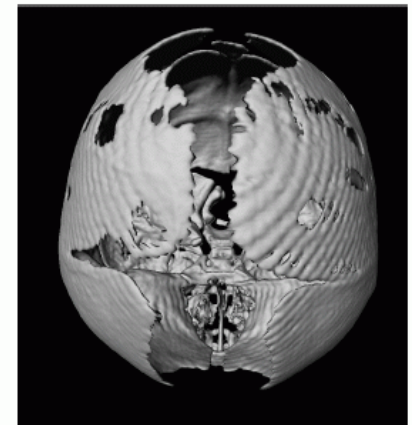
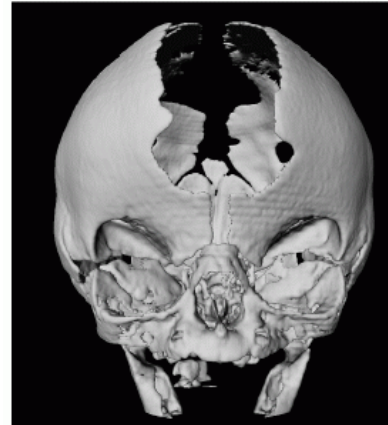
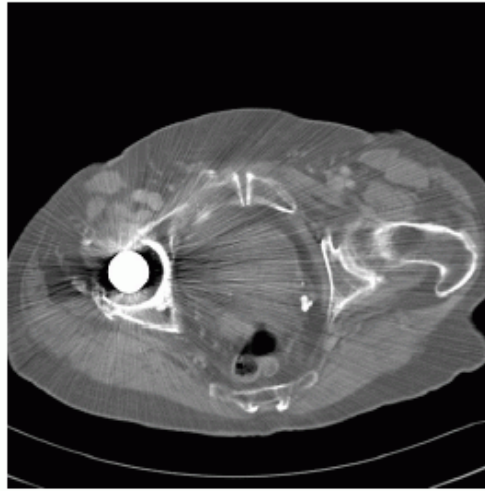
- rod moved during acquisition



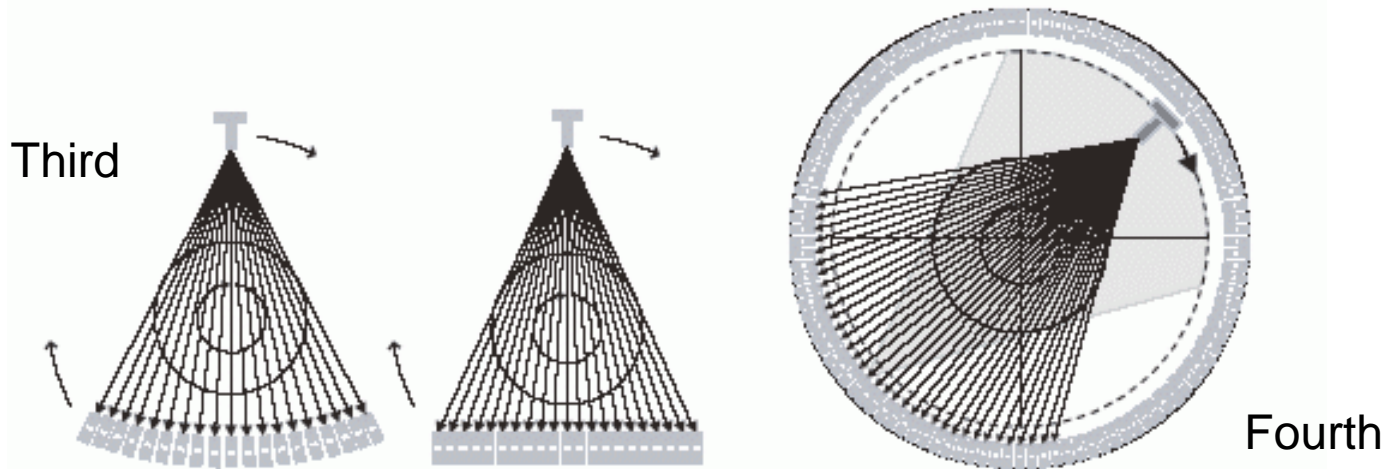
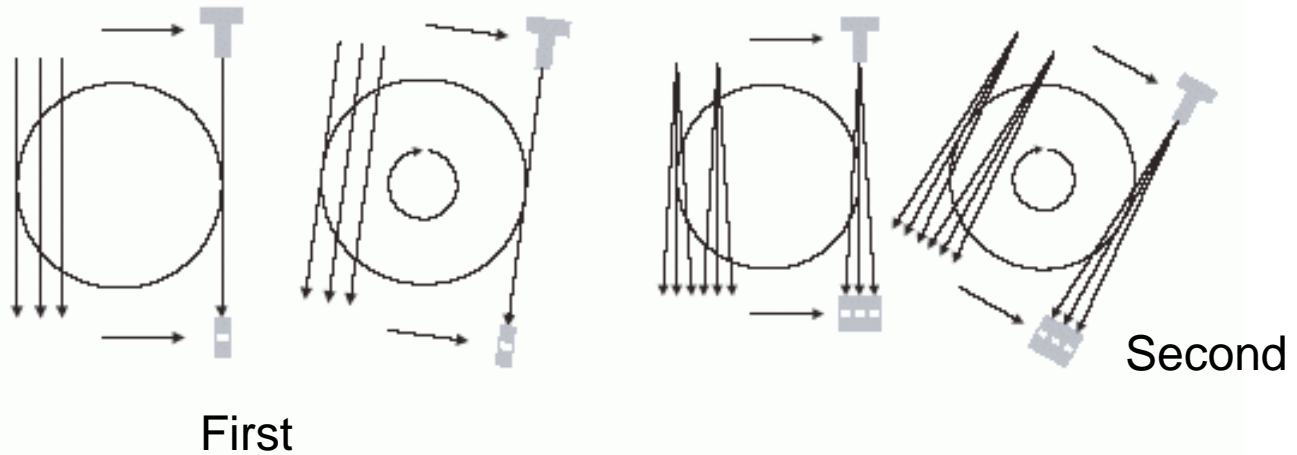
Stair step artifacts:

- the helical acquisition path becomes visible in the reconstruction:

Many artifacts combined:



Scanner Generations



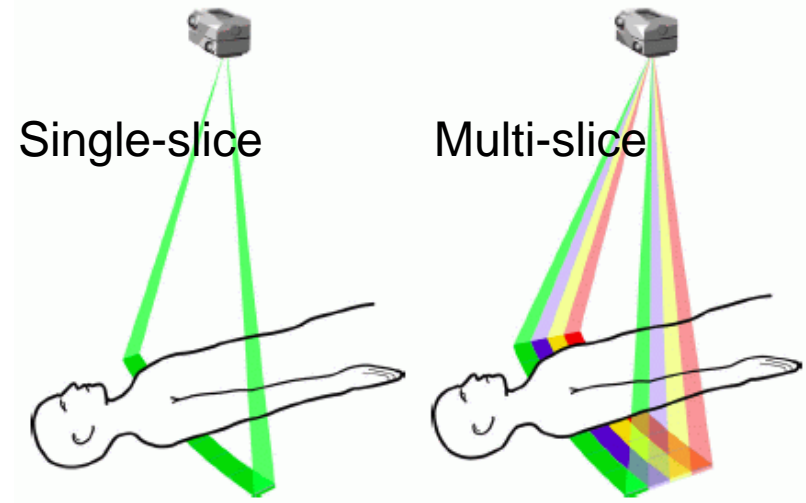
Third generation most popular since detector geometry is simplest

- collimation is feasible which eliminates scattering artifacts

Multislice CT

Nowadays (spiral) scanners are available that take up to 256 simultaneous slices (GE LightSpeed, Siemens, Phillips, Toshiba)

- require cone-beam algorithms for *fully-3D* reconstruction
- exact cone-beam algorithms have been recently developed



Multi-slice scanners enable faster scanning

- recall cone-beam?
- image lungs in 15s (one breath-hold)
- perform dynamic reconstructions of the heart (using gating)
- pick a certain phase of the heart cycle and reconstruct slabs in z

Multislice CT

Enables scanning of dynamic phenomena

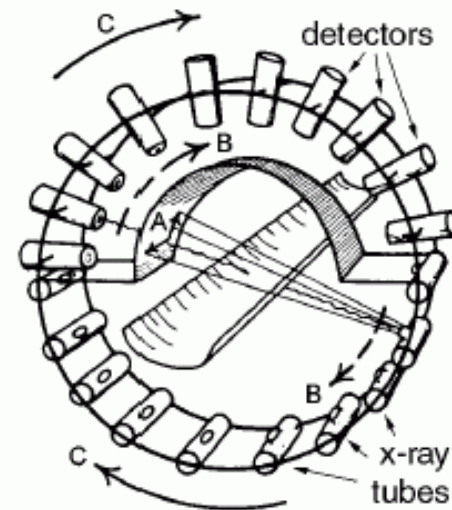
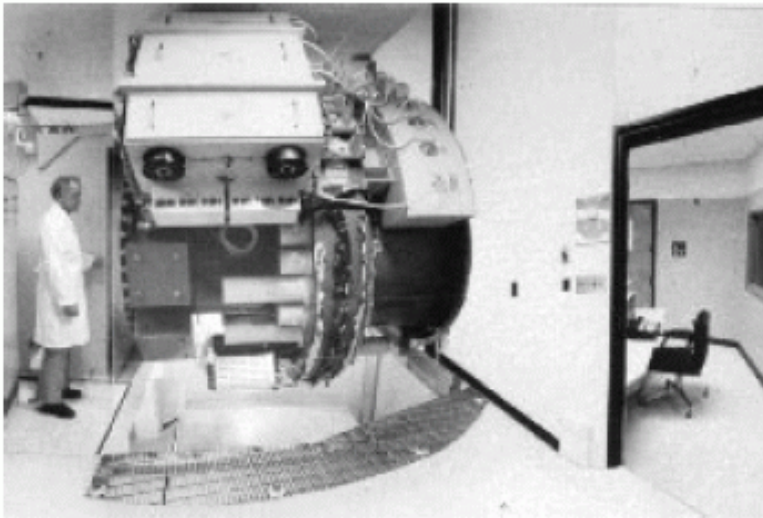
- cardiac scanning
- lung scanning



Exotic Scanners: Dynamic Spatial Reconstructor

Dynamic Spatial Reconstructor (DSR)

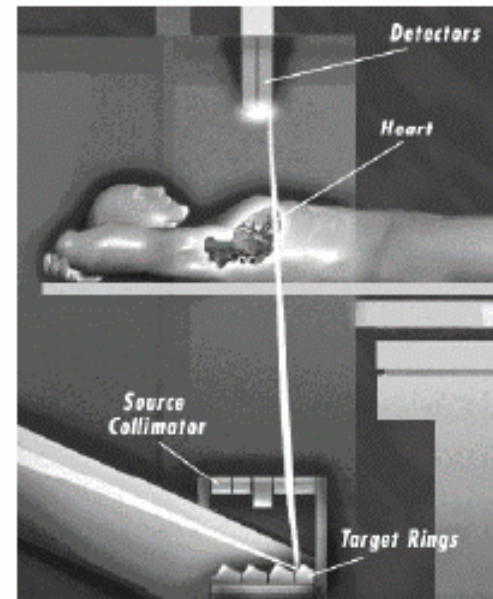
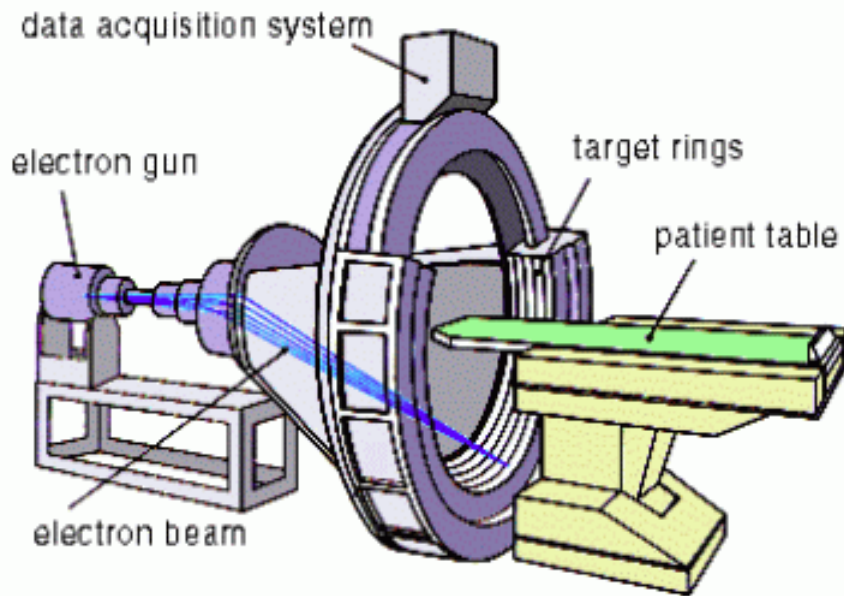
- first fully 3D scanner, built in the 1980s by Richard Robb, Mayo Clinic
- 14 source-detector pairs rotating
- acquires data for 240 cross-sections at 60 volume/s
- 6 mm resolution (6 lp/cm)



Exotic Scanners: Electron Beam

Electron Beam Tomography (EBT)

- developed by Imatron, Inc
- currently 80 scanners in the world
- no moving mechanical parts
- ultra-fast (32 slices/s) and high resolution (1/4 mm)
- can image beating heart at high resolution
- also called cardiovascular CT CT (fifth generation CT)



CT: Final Remarks

Applications of CT

- head/neck (brain, maxillofacial, inner ear, soft tissues of the neck)
- thorax (lungs, chest wall, heart and great vessels)
- urogenital tract (kidneys, adrenals, bladder, prostate, female genitals)
- abdomen (gastrointestinal tract, liver, pancreas, spleen)
- musculoskeletal system (bone, fractures, calcium studies, soft tissue tumors, muscle tissue)

Biological effects and safety

- radiation doses are relatively high in CT (effective dose in head CT is 2mSv, thorax 10mSv, abdomen 15 mSv, pelvis 5 mSv)
- factor 10-100 higher than radiographic studies
- proper maintenance of scanners a must

Future expectations

- CT to remain preferred modality for imaging of the skeleton, calcifications, the lungs, and the gastrointestinal tract
- other application areas are expected to be replaced by MRI (see next lectures)
- low-dose CT and full cone-beam can be expected