

# Estimation of Multiple Illuminants from a Single Image of Arbitrary Known Geometry\*

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## Overview

### ■ Assumptions

- ◆ Lambertian object of arbitrary known geometry
- ◆ Directional light sources

$$L = \mathbf{a} \cdot \mathbf{I} \cdot \mathbf{n}$$

### ■ Advantages

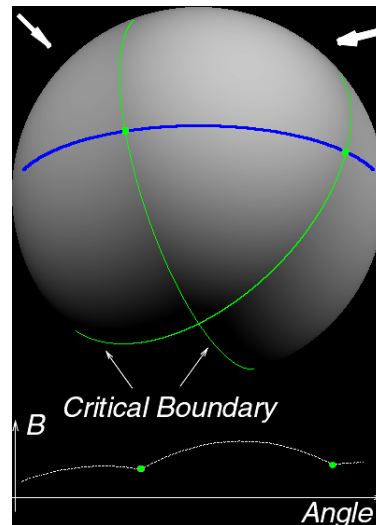
- ◆ Single image
- ◆ No need for particular calibration objects
- ◆ Robust to noise
- ◆ Use of global information more suitable to Lambertian surfaces

## Related Work

- Critical Points & Occluding Boundaries:  
Yang et al., CVPR'91 [20]  
Zhang et al., CVPR'00 [21]
  - ◆ Sensitive to noise. Needs calibration object
- Convolution  
Basri et al., ICCV'01 [1]  
Ramamoorthi et al., SIGGRAPH'01 [15]
  - ◆ Can not compute exact positions of directional light sources on Lambertian Surfaces
- Specular Sphere  
Debevec, SIGGRAPH'98 [3]
  - ◆ Interacts with environment. Need calibration object

## Basic Definitions

- Critical Point
  - ◆ A point in the image is called a **critical point** if the surface normal at the corresponding point on the surface of the object is perpendicular to one of the light sources.
- Critical Boundary
  - ◆ All critical points corresponding to a real light will be grouped into a cut-off curve which is called a **critical boundary**.
  - ◆ Circle of maximum circumference on the sphere.

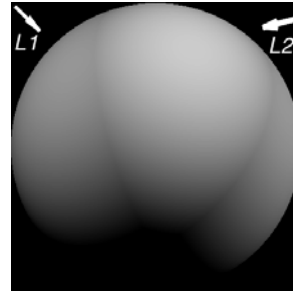


■ 2 Light Sources

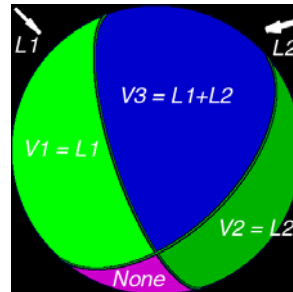
## Real Light Source Detection

- Virtual Light Patch
  - ◆ Critical boundaries will segment the whole sphere image into several regions. Each segmented region corresponds to one virtual light that minimizes  $\sum_i (I_i - L \cdot N_i)^2$ . Each region is called a **virtual light patch**.
- Intuitively, the **difference** between two virtual lights is caused by a real light source, e.g.,

$$v3 - v1 = (L1 + L2) - L1 = L2$$



■ Input Image

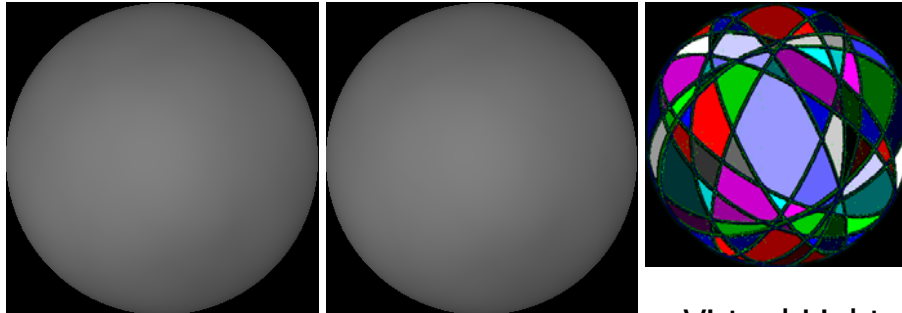


■ Segmented Image

## Our Algorithm

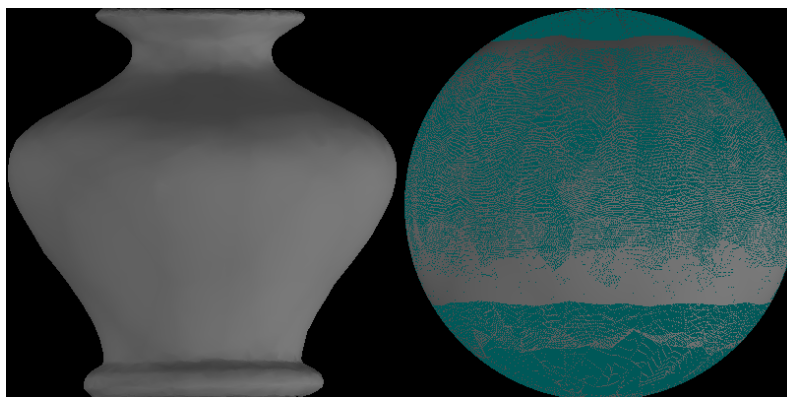
1. Detect critical points.
2. Find initial critical boundaries by Hough transform.
3. Adjust critical boundaries. Adjust every critical boundary by moving it by a small step, and a reduction in the least-squares error indicates a better solution. Update boundaries using a “greedy” algorithm to minimize the total error.
4. Merge spurious critical boundaries. If two critical boundaries are closer than a threshold angle (e.g. 5 degrees), they can be replaced by their average.
5. Remove spurious critical boundaries. Test every critical boundary, and remove it if the least-squares error does not increase. Test boundaries in increasing order of Hough transform votes (first test boundaries that are not as trustworthy).
6. Calculate the real lights along a boundary by subtracting neighboring virtual lights.

## Synthetic Sphere – 15 Light Sources



- Original Image
- Rerendered Image
- Virtual Light Patches
- Average Pixel Intensity (0-255 range) Error: 0.42 gray levels

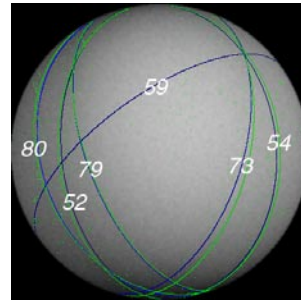
## Objects of Arbitrary Geometry



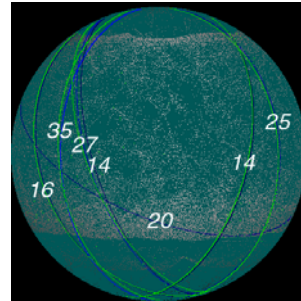
- Normals are mapped to a sphere
- High number of missing data points on the sphere (in green)

# Hough Transform

- Use global information to get boundaries.
- Problems:
  - ◆ Noise causes fake boundaries.
  - ◆ Sparse data cause missing boundaries.
- Solution:
  - ◆ Evaluating the Least-Squares error using information from every available pixel inside a region (virtual light patch).



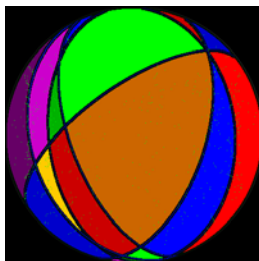
■ Lambertian Ball



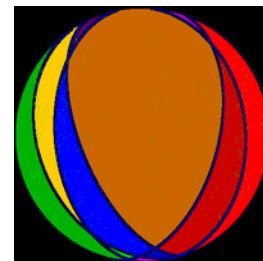
■ Lambertian Vase

# Virtual Light Patches

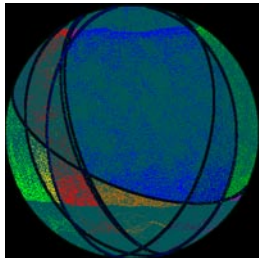
- Lambertian Ball



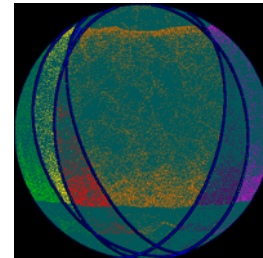
- One spurious critical boundary is removed



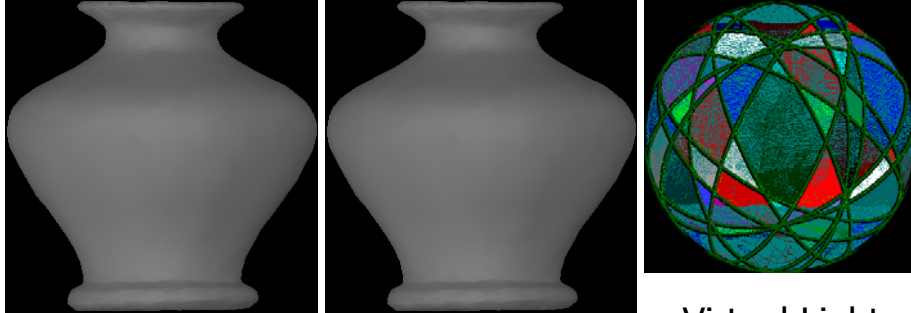
- Lambertian Vase



- One spurious critical boundary is removed
- Two critical boundaries are merged



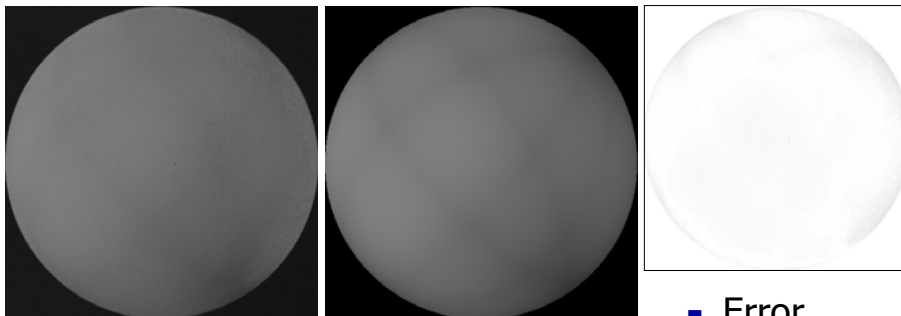
## Synthetic Vase – 15 Light Sources



- Original Image
- Rerendered Image
- Virtual Light Patches

■ Average Pixel Intensity (0-255 range) Error:  
0.74 gray levels

## Real Image of a Rubber Ball – 5 Light Sources

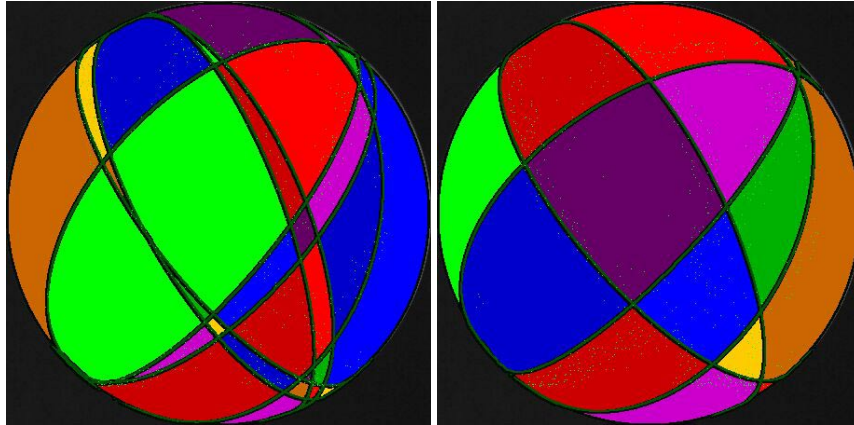


- Original Image
- Rerendered Image
- Error Image

■ Average Pixel Intensity (0-255 range) Error:  
3.39 gray levels

## Real Image of a Rubber Ball

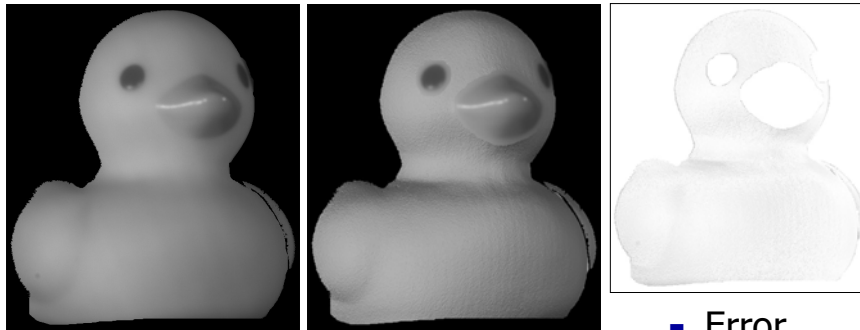
– 5 Light Sources



■ Initial and Final Virtual Light Patches

## Real Image of a Rubber Duck

– 4 Light Sources

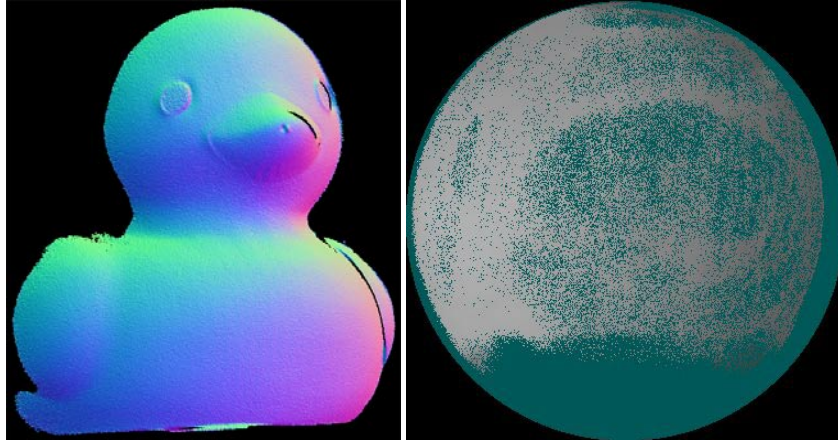


■ Original Image   ■ Rerendered Image   ■ Error Image  
■ Average Pixel Intensity (0-255 range) Error:  
6.55 gray levels



## Real Image of a Rubber Duck

– 4 Light Sources

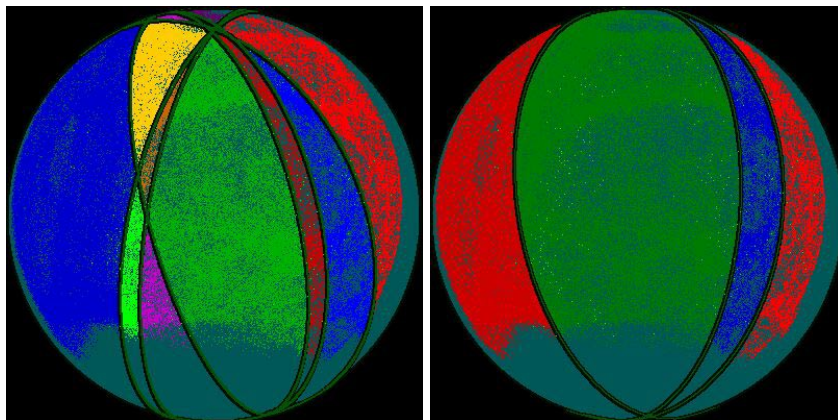


■ 3D Shape  
(Noise in acquisition)

■ Sphere mapping

## Real Image of a Rubber Duck

– 4 Light Sources



■ Initial patches

■ Final patches



## Future Work

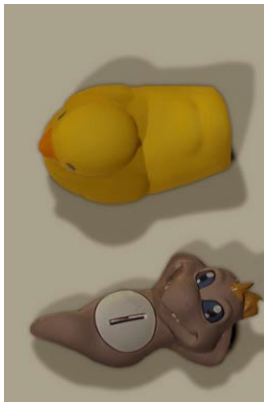
- Study of the properties of arbitrary surfaces, so that we can avoid the intermediate sphere mapping.
- Speed up of the least-squares method.
- Extend the method to non-Lambertian diffuse reflectance for rough surfaces.
- Explore combinations of our method with shadow based light estimation methods and with specular detection methods.

## Future Work (Preview)

- Augmented Reality Application– 3 Light Sources



■ Original Image



■ Rerendering with one light switched off



■ Superimposing an object